

# Study of neutrino oscillations in the long base-line experiment K2K

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# Outline

Phenomenology of neutrino oscillations

K2K

principles of the experiment

detectors

performance

analysis

results

Neutrino oscillations: status and problems

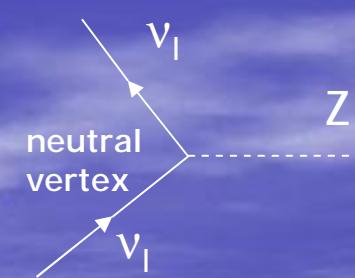
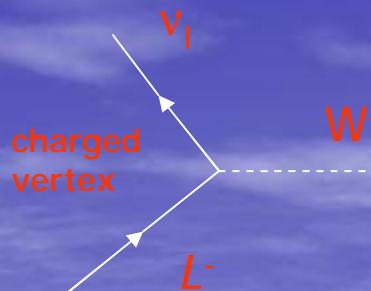
T2K

Near future

# Leptons

$$\begin{pmatrix} e \\ n_e \end{pmatrix} \begin{pmatrix} m \\ n_m \end{pmatrix} \begin{pmatrix} t \\ n_t \end{pmatrix} \xrightarrow{\text{EM, weak}} \text{EM, weak}$$

$$\xrightarrow{\text{weak}}$$



two different neutrino bases

Flavor states  
produced via  
charged currents

$$\begin{array}{ccc} n_e & n_m & n_t \\ L_e = +1 & L_\mu = +1 & L_\tau = +1 \end{array}$$

Mass eigenvalues  
Mass eigenstates

$$\begin{array}{c} m_i \\ |n_i\rangle \end{array}$$

flavor eigenstates  $|n_a\rangle$       <sup>1</sup> mass eigenstates  $|n_i\rangle$

Unitary transformation:  $|n_a\rangle = U_{ai} |n_i\rangle$

$U_{ai}$  - neutrino(lepton) mixing matrix

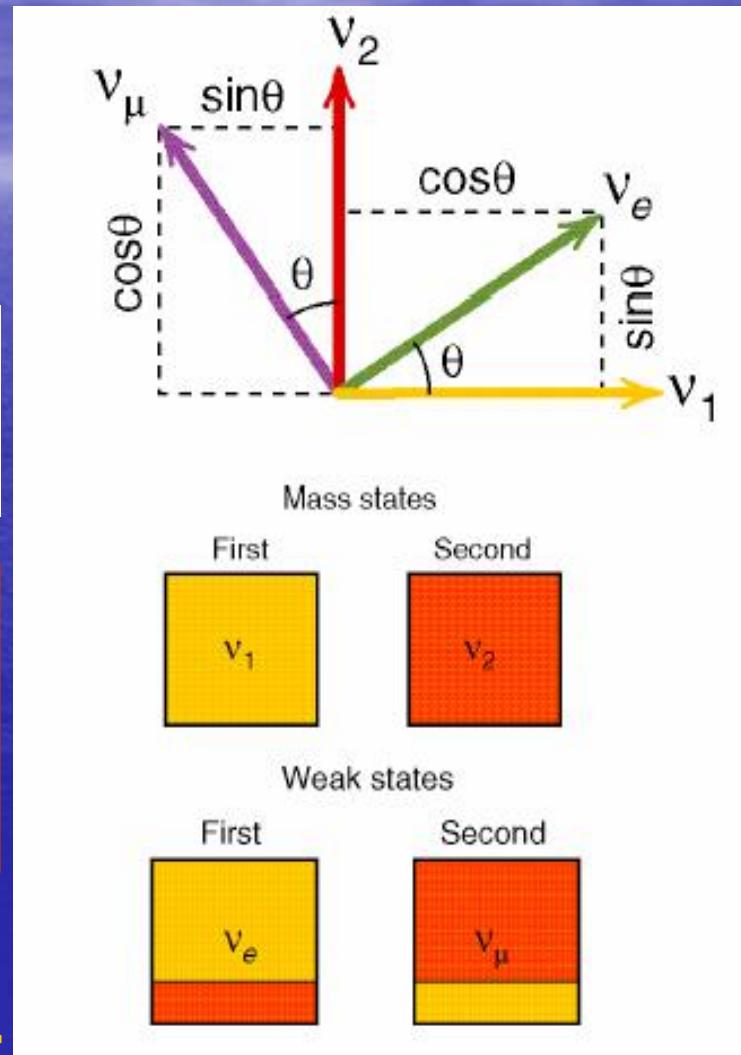
# Mixing in two families

Consider for simplicity two families.  
Mixing matrix depends of a single parameter, the mixing angle  $\theta$

The weak and mass eigenstates are connected by a simple two-dimensional rotation

$$\begin{pmatrix} n_e \\ n_m \end{pmatrix} = \begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} n_1 \\ n_2 \end{pmatrix} = U \begin{pmatrix} n_1 \\ n_2 \end{pmatrix}$$

$$n_e = \cos\theta |n_1\rangle + \sin\theta |n_2\rangle$$
$$n_m = -\sin\theta |n_1\rangle + \cos\theta |n_2\rangle$$



# Neutrino oscillations



The weak interaction produces neutrinos of a given flavor

Distance  $x_0 = 0$  time  $t=0$

$$\begin{aligned} |\mathbf{n}(x_0)\rangle &= |\mathbf{n}_e\rangle \\ &= \cos q |\mathbf{n}_1\rangle + \sin q |\mathbf{n}_2\rangle \end{aligned}$$

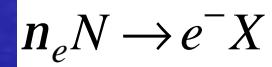
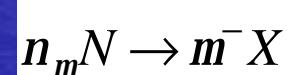
The mass eigenstates propagate at different velocities

Distance  $x$  time  $t$



$$|\mathbf{n}_e\rangle_t = \cos q \exp(ip_1 x) \exp(-iE_1 t) |\mathbf{n}_1\rangle + \sin q \exp(ip_2 x) \exp(-iE_2 t) |\mathbf{n}_2\rangle$$

Detection via weak interactions



$$P(n_e \rightarrow n_m) = |\langle \mathbf{n}_m | \mathbf{n}(t) \rangle|^2$$

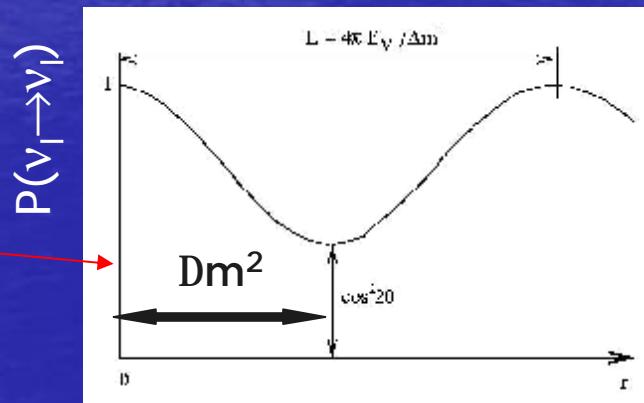
# Oscillation formalism

$$E^2 = p^2 + m^2 \quad \text{neutrino: } p \gg m \rightarrow E \approx p + m^2/2p \quad E_2 - E_1 = Dm^2/2E$$

$$Dm^2 = |m_1^2 - m_2^2| \quad E \gg p$$

$$\begin{aligned} P(n_e \rightarrow n_m) &= |<n_m | n(L)>|^2 = \left| -sce^{-i\frac{m_1^2}{2E}L} + cse^{-i\frac{m_2^2}{2E}L} \right|^2 \\ &= 4s^2c^2(1 - \cos \frac{m_1^2 - m_2^2}{2E}L) = \sin^2(2q)\sin^2(\frac{\Delta m_{12}^2}{4E}L) \end{aligned}$$

$$P(v_\mu \rightarrow v_\mu) = 1 - P(v_\mu \rightarrow v_x)$$



$$P(n_m \rightarrow n_x) = \sin^2 2q \sin^2 [1.27 Dm^2 (\text{eV}^2) L (\text{km}) / E_n (\text{GeV})]$$

$$P(n_m \rightarrow n_m) = 1 - \sin^2 2q \sin^2 [1.27 Dm^2 (\text{eV}^2) L (\text{km}) / E_n (\text{GeV})]$$

# PMNS mixing matrix

3 families

$$\begin{pmatrix} \mathbf{n}_e \\ \mathbf{n}_m \\ \mathbf{n}_t \end{pmatrix} = U \begin{pmatrix} \mathbf{n}_1 \\ \mathbf{n}_2 \\ \mathbf{n}_3 \end{pmatrix} \quad U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{m1} & U_{m2} & U_{m3} \\ U_{t1} & U_{t2} & U_{t3} \end{pmatrix}$$

$U$  parameterization

three mixing angles  $\theta_{12}$   $\theta_{13}$   $\theta_{23}$   
complex phase  $\delta$

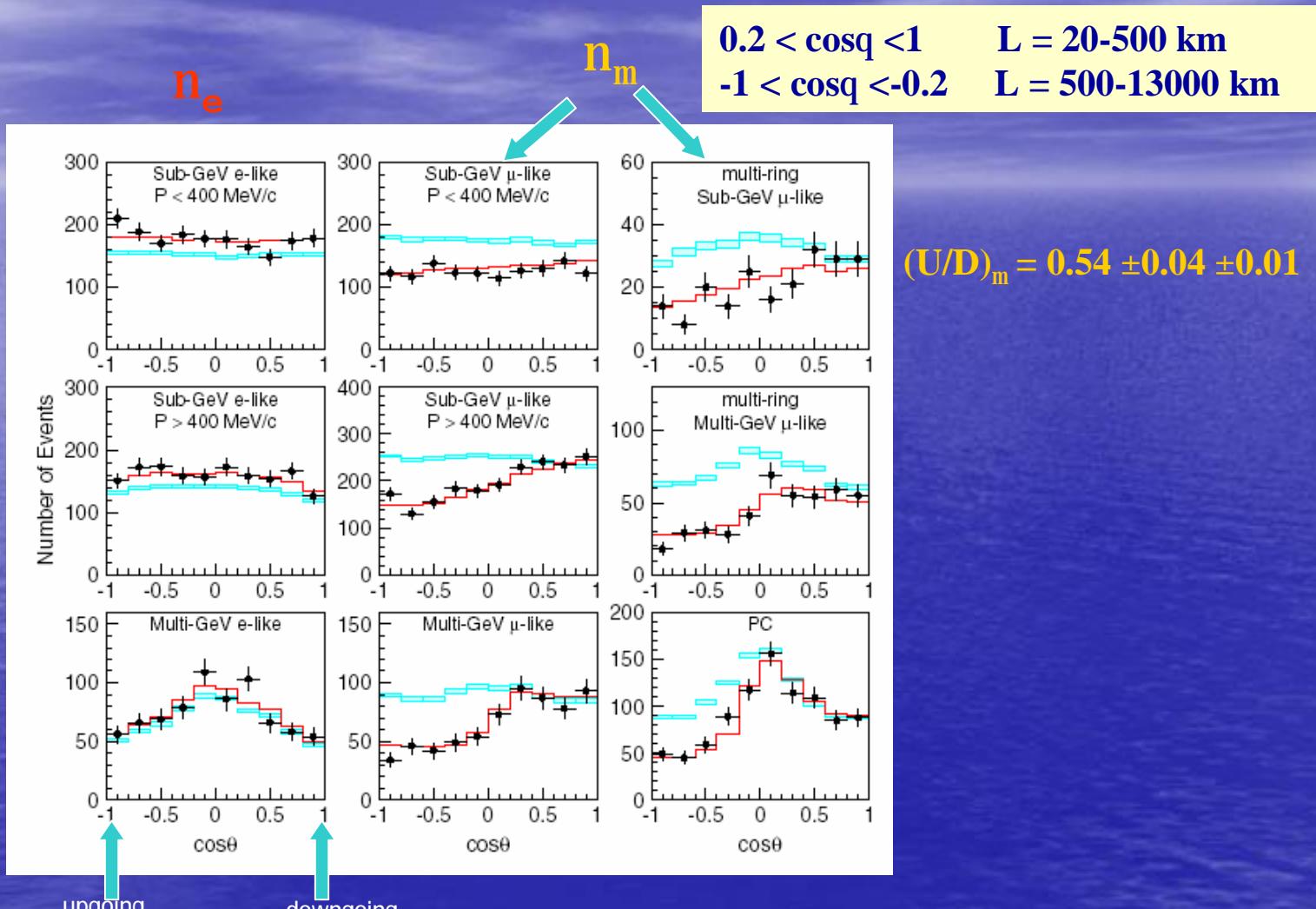
$$\frac{|U_{e2}|^2}{|U_{e1}|^2} = \tan^2 q_{12} \quad \frac{|U_{m3}|^2}{|U_{t3}|^2} = \tan^2 q_{23} \quad U_{e3} = \sin q_{13} e^{-i\delta}$$

$$\Delta m_{ij}^2 = m_i^2 - m_j^2 \quad \Delta m_{12}^2 + \Delta m_{23}^2 + \Delta m_{31}^2 = 0 \quad \rightarrow \text{two independent } \Delta m^2$$

$$\Delta m_{12}^2 = \Delta m_{sol}^2 \quad \Delta m_{23}^2 \cong \Delta m_{31}^2 = \Delta m_{atm}^2$$

# Atmospheric neutrino oscillations

SK



**SK:**  $n_m$  oscillation with  $\Delta m^2 \sim (2\text{-}3) \times 10^{-3} \text{ eV}^2$

# Main goal of K2K

First accelerator long base-line neutrino experiment

Measurement of (search for)  
neutrino oscillations in  
LBL accelerator experiment  
to confirm the oscillation  
observed by the SuperKamiokande

$$\Delta m^2 \sim (2-3) \times 10^{-3} \text{ eV}^2 \quad \sin 2\theta \sim 1$$

# Experiment K2K

Collaboration K2K: Japan-USA-Korea-Canada-Russia-France-Italy-Spain-Switzerland

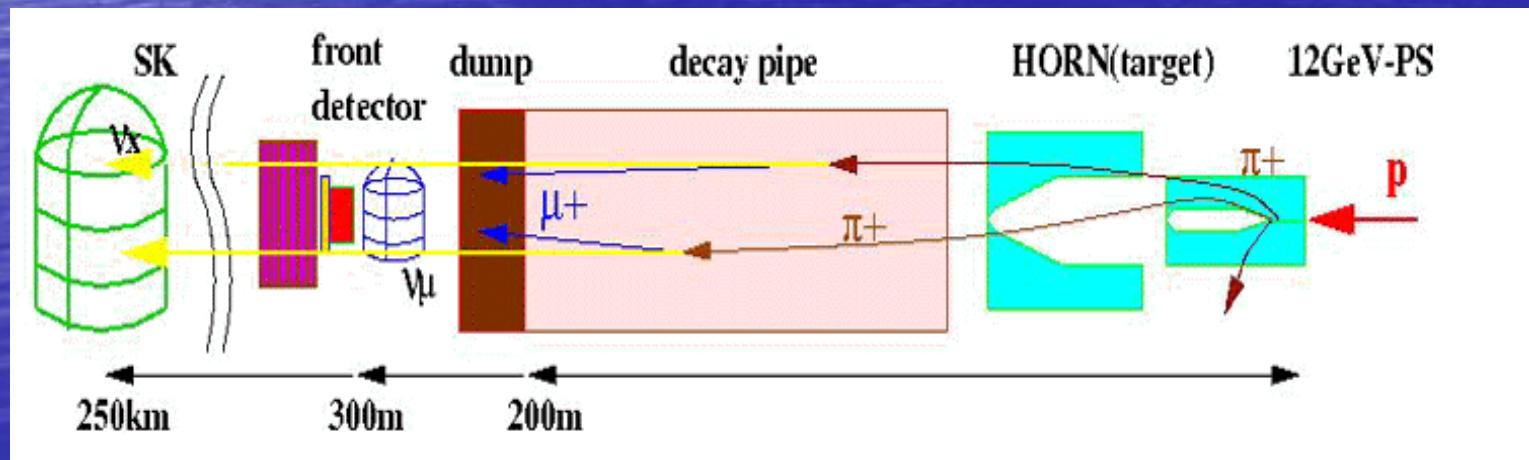
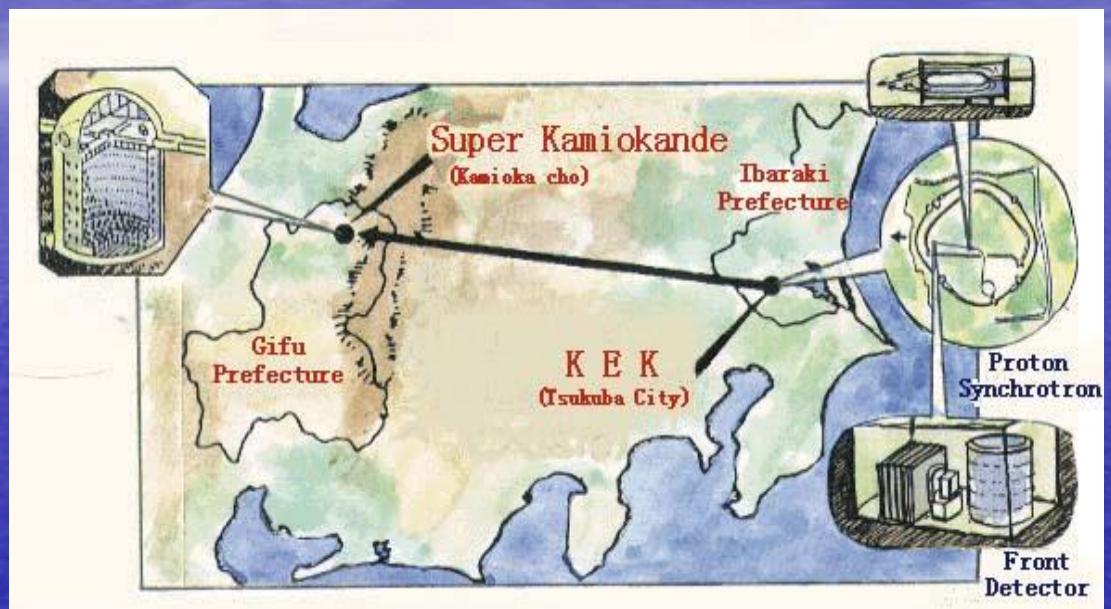
$$n_m \gtrless n_t \quad (n_m \gtrless n_x)$$

$$L/E_n \gg 200$$

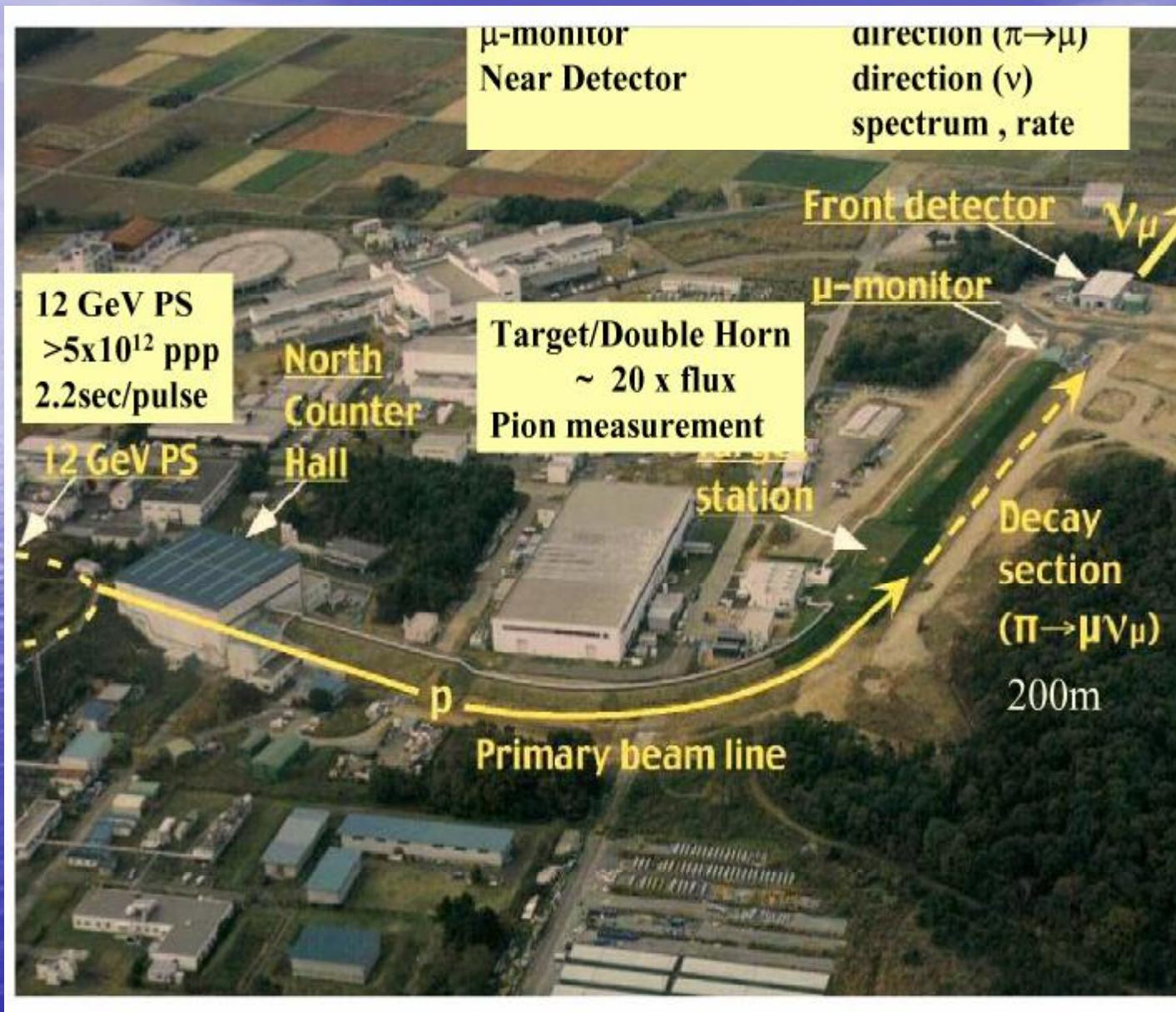
$$L=250 \text{ km} \quad \langle E_n \rangle \gg 1.3 \text{ GeV}$$

$$\begin{array}{ll} n_m & 98.2\% \\ n_e & 1.3\% \end{array}$$

$$Dm^2 \approx 2 \cdot 10^{-3} \text{ eV}^2$$

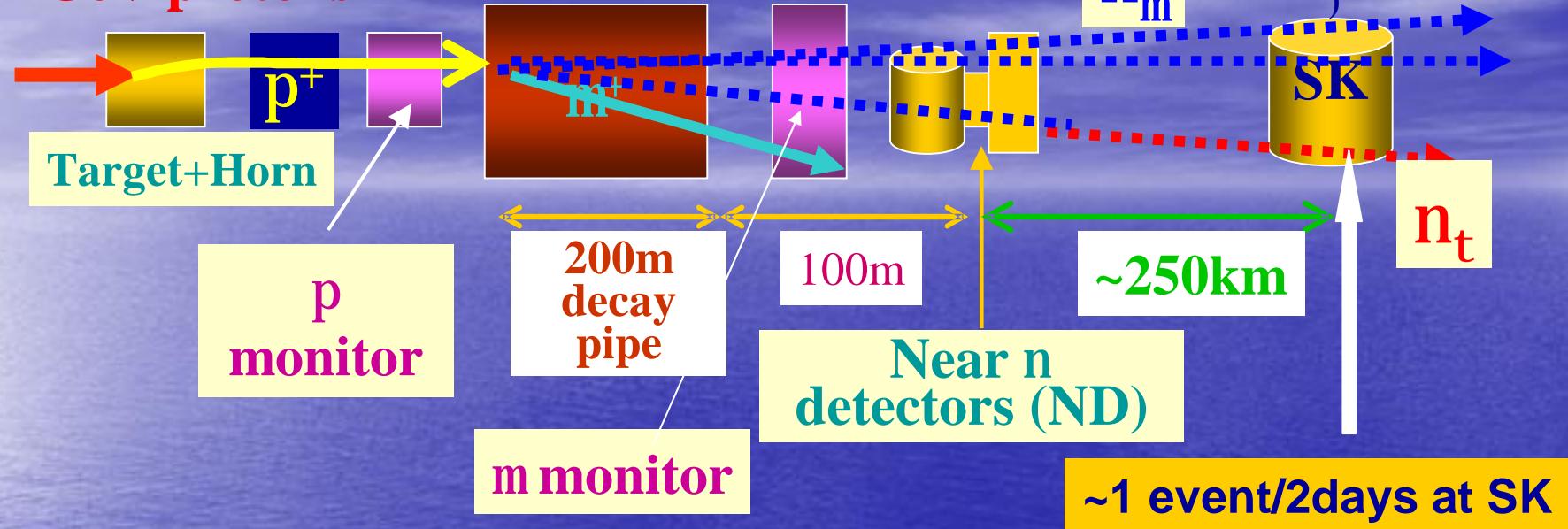


# K2K Beam Line



# K2K principles

12GeV protons



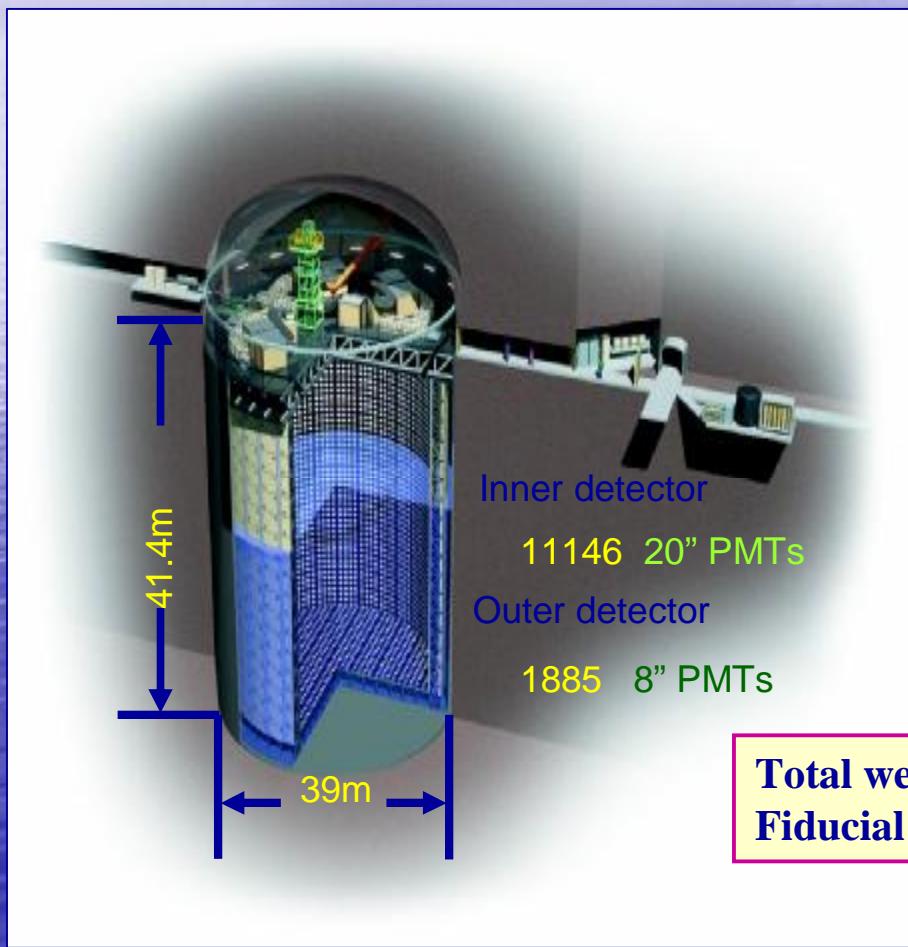
Far/Near ratio (by MC)  $\sim 10^{-6}$

## Signal of n oscillation

- | Reduction of  $n_m$  events
- | Distortion of  $n_m$  energy spectrum

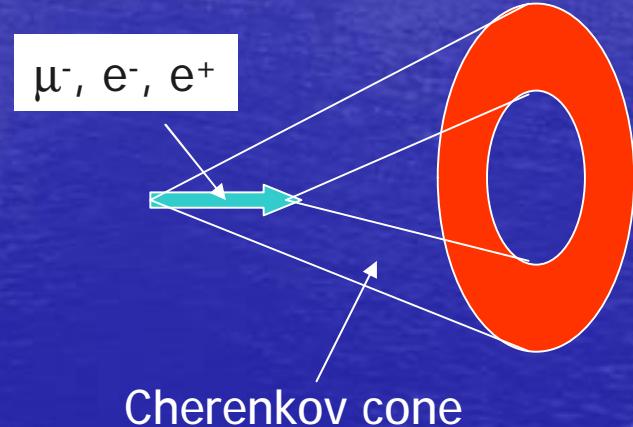
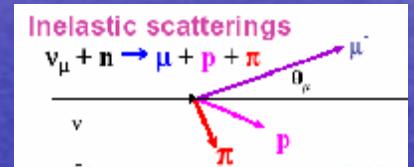
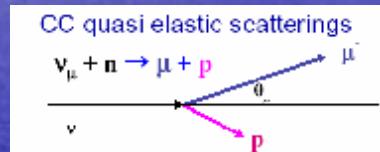
# Far detector

## Super-Kamiokande I



## Super-Kamiokande II

~5200 PMTs  
with FRP+Acrylic cover



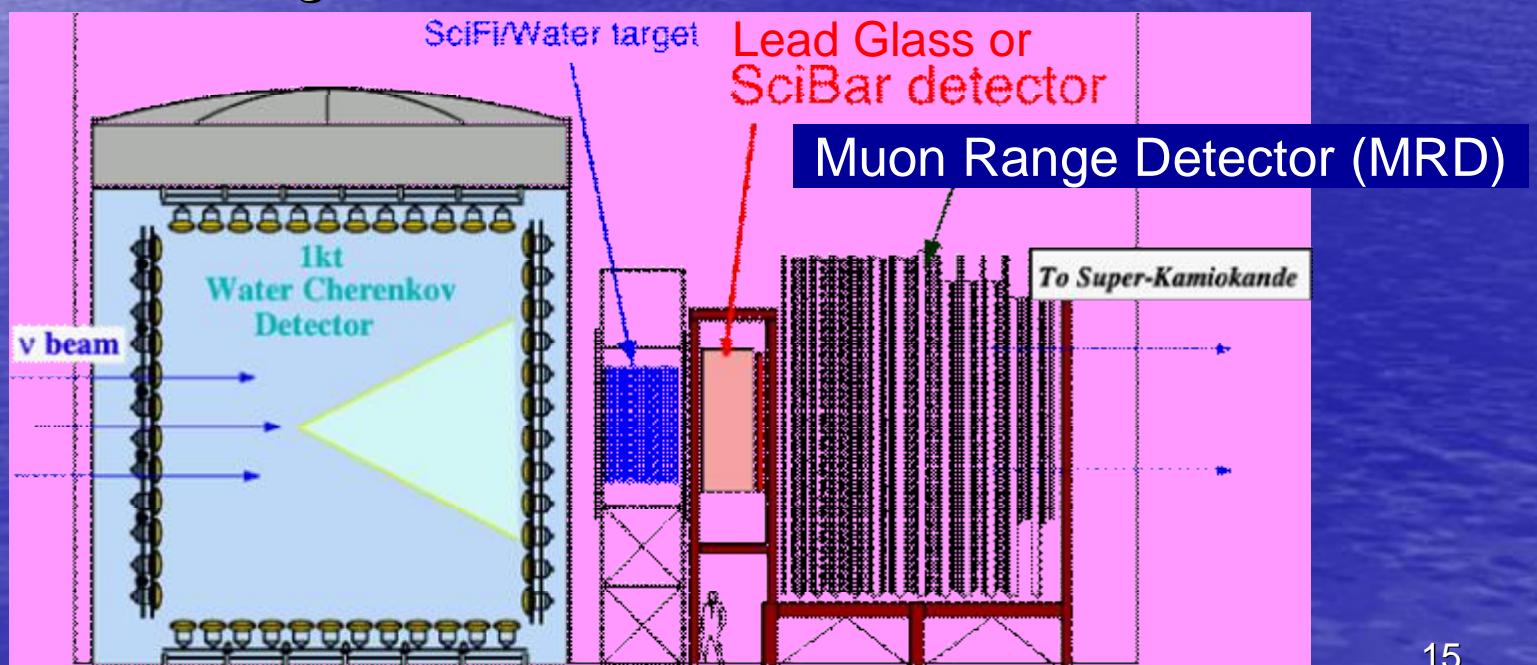
SK events

m - like

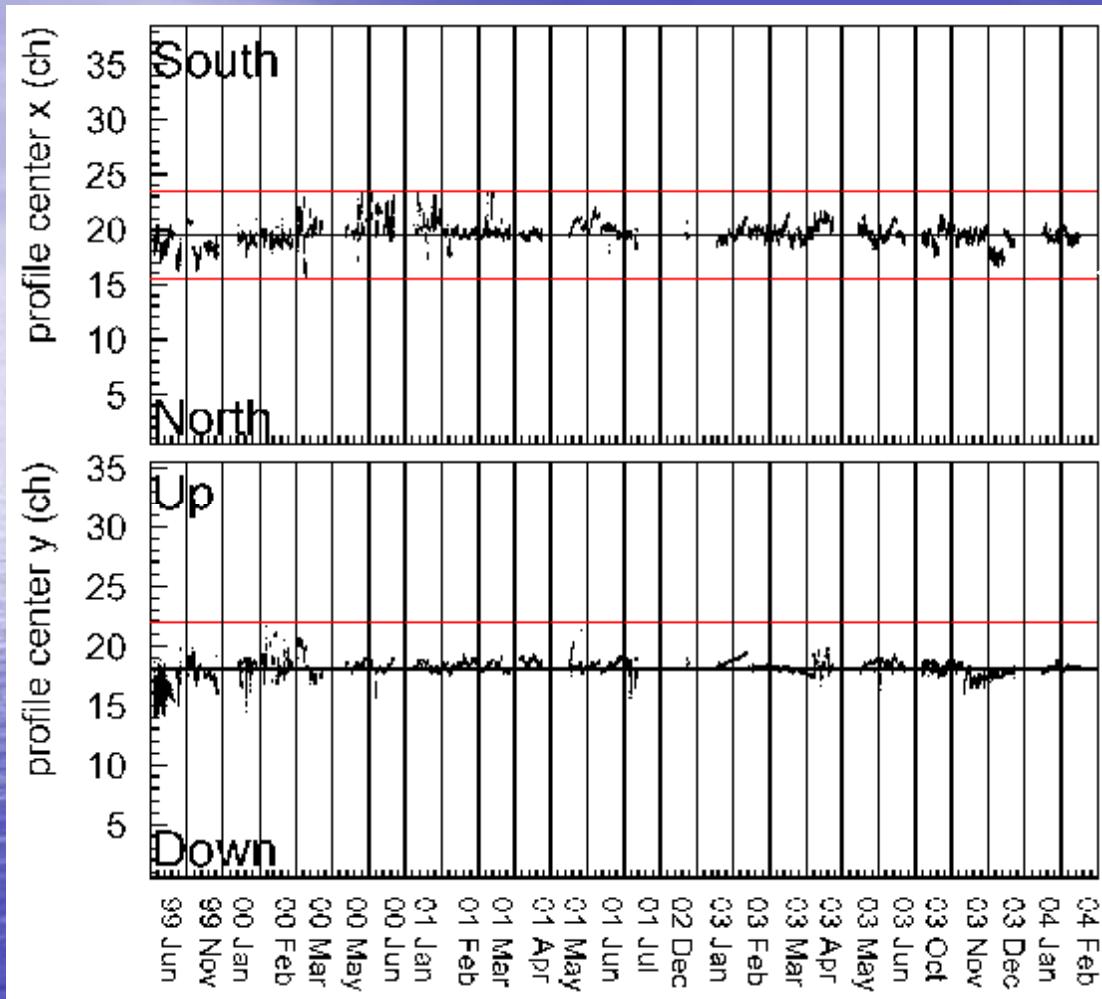
e - like

# Near Detectors

- **1KT**: water Cherenkov detector [25t fiducial]
- **SciFi**: scintillating fiber and water target [6t fiducial]
- **LG**: Lead glass calorimeter (removed in 2002)
- **SciBar**: fully-active scintillator detector [10t fiducial]  
(installed in 2003)
- **MRD**: muon range detector

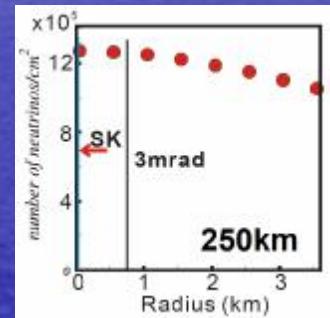


# Beam stability (muon monitor)



+ 1 mrad

- 1 mrad



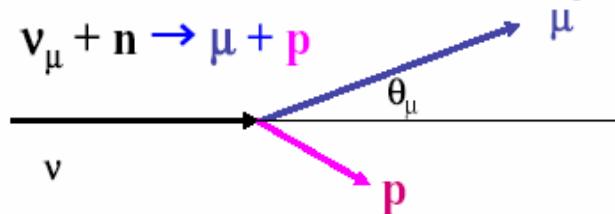
+ 1 mrad

- 1 mrad

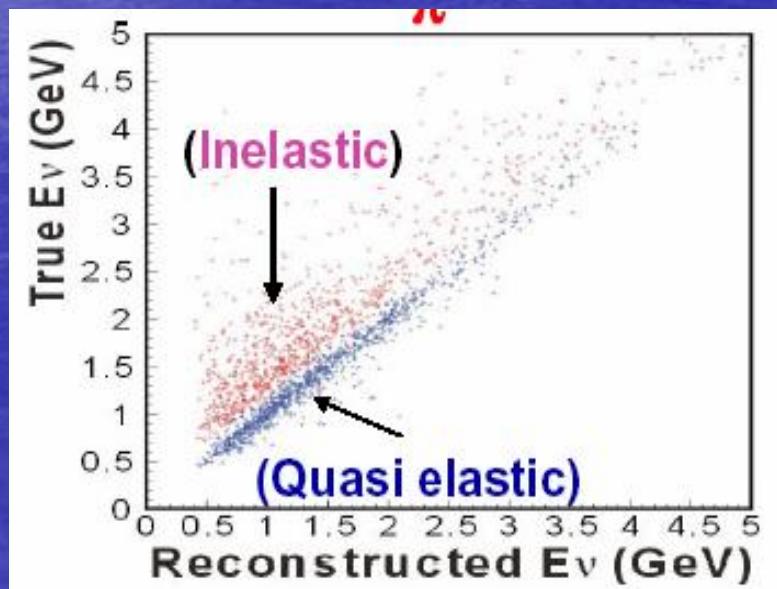
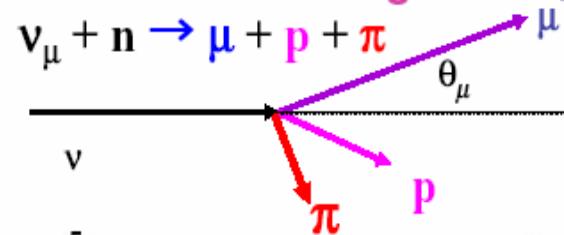
- muon profile is monitored spill-by-spill
- muon center is stable within 1mrad.

# Neutrino energy reconstruction

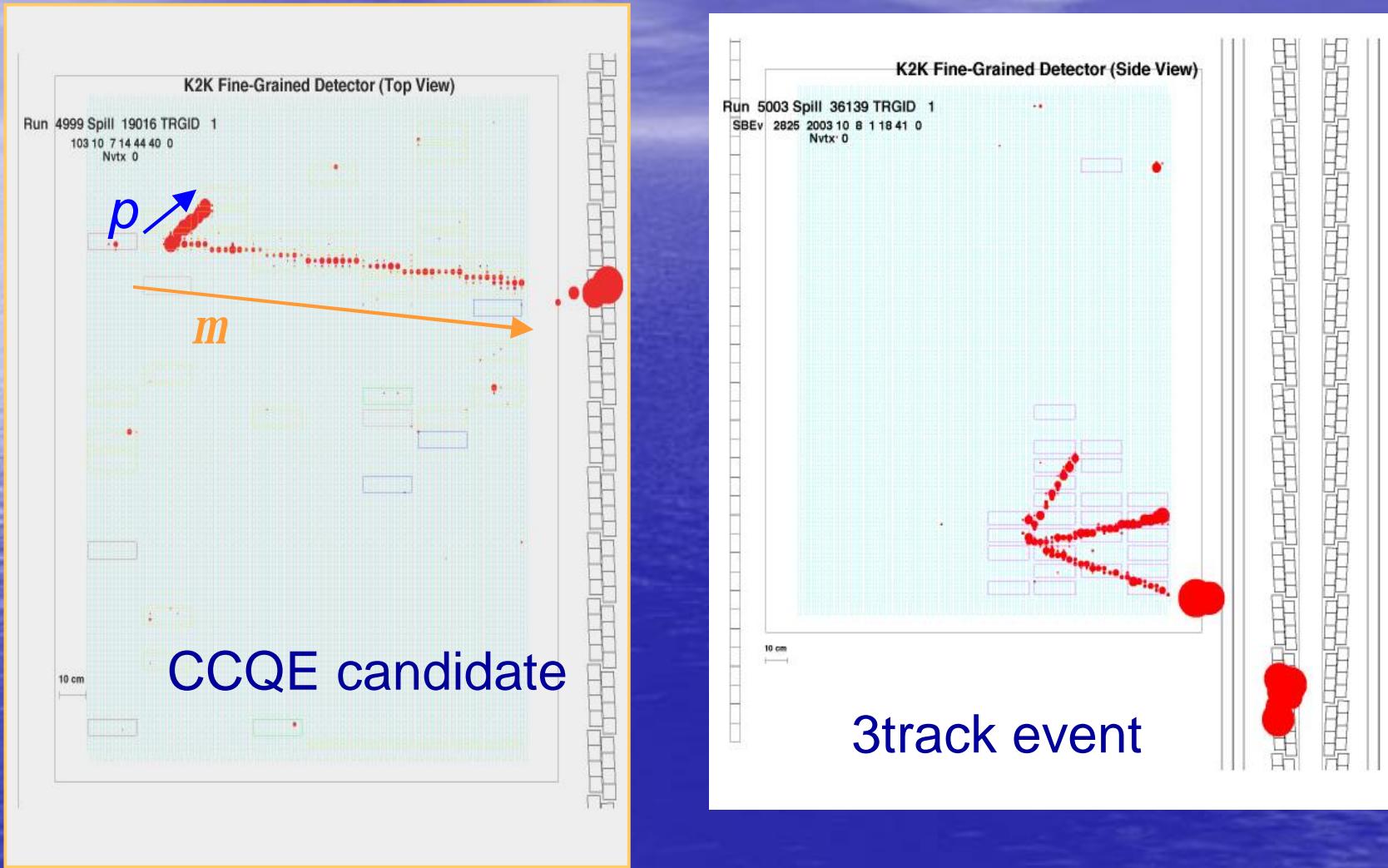
CC quasi elastic scatterings



Inelastic scatterings



# SciBar Event Display



# Measurements at ND

- 1KT :  $P_\mu < 1.5 \text{ GeV}/c$ ,  $4\pi$  acceptance  
– 1-ring  $\mu$ -like ( $1R\mu$ ) fully contained  
in Fiducial volume 25 ton (FC) :

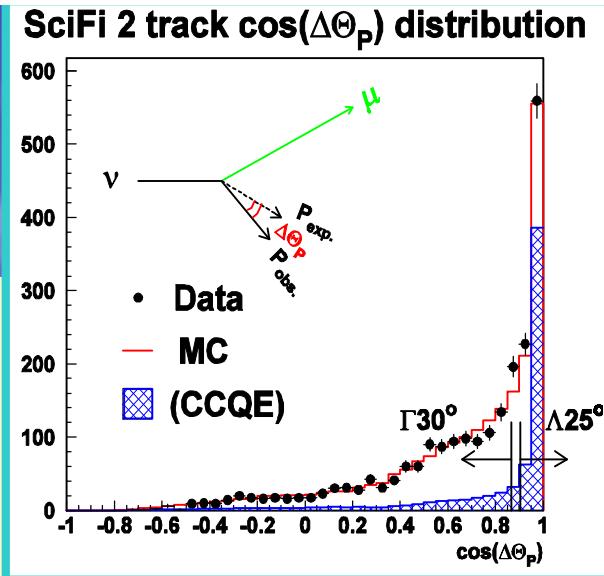
- SciFi :  $P_\mu > 0.55 \text{ GeV}/c$ ,  $\theta_\mu < 60 \text{ deg}$ . Fid volume 5.6 t  
– 1-track  $\mu$ -like : QE-like ( $\Delta\theta_p < 25 \text{ deg}$ ) :  
nonQE-like ( $\Delta\theta_p > 30 \text{ deg}$ ) :

- Scibar :  $P_\mu > 0.45 \text{ GeV}/c$  Fid. volume 9.4 t

- PIMON

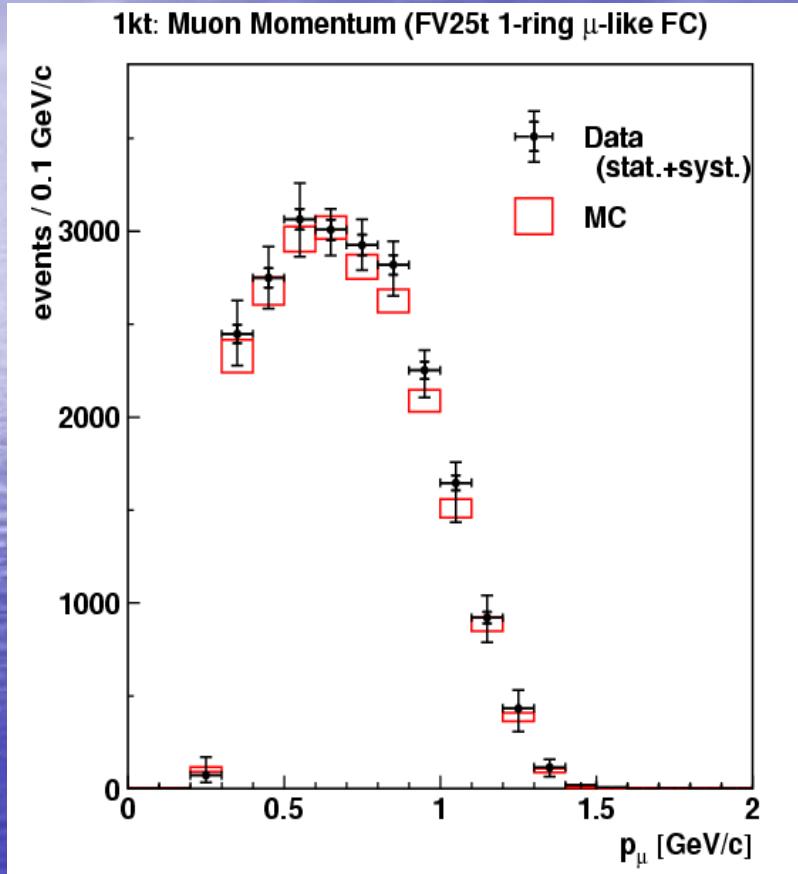
$(p, \theta)$  distribution  $\Rightarrow$  Neutrino Spectrum ( $> 1 \text{ GeV}$ ) Fitting Parameters

$E_\nu$  : 8 bins, nonQE/QE ratio : 1

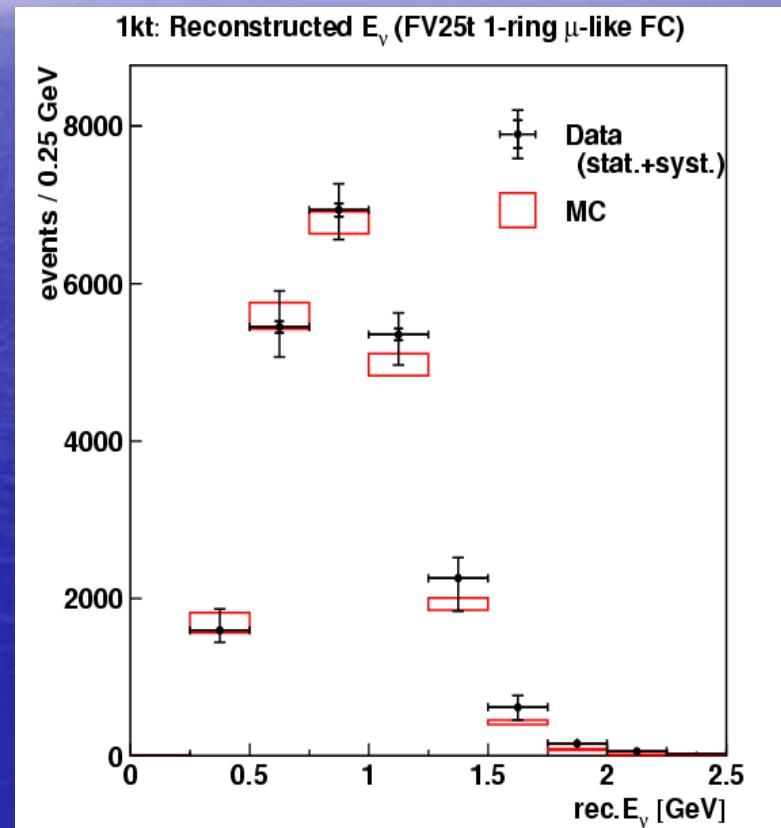


# 1kT spectra

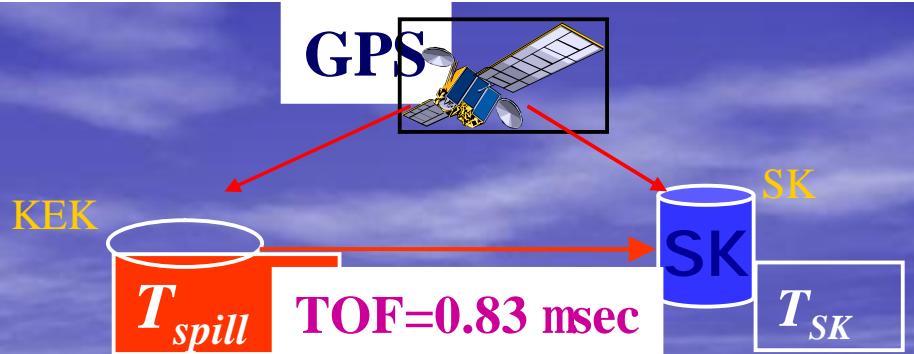
1 ring m-like



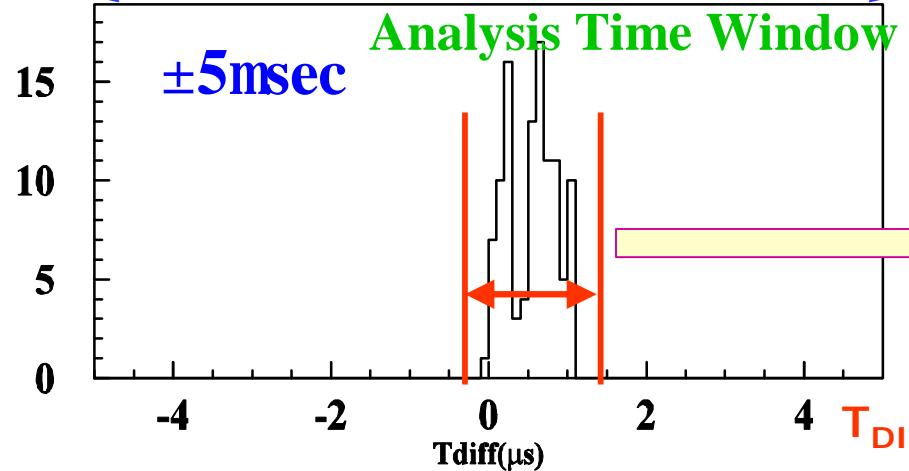
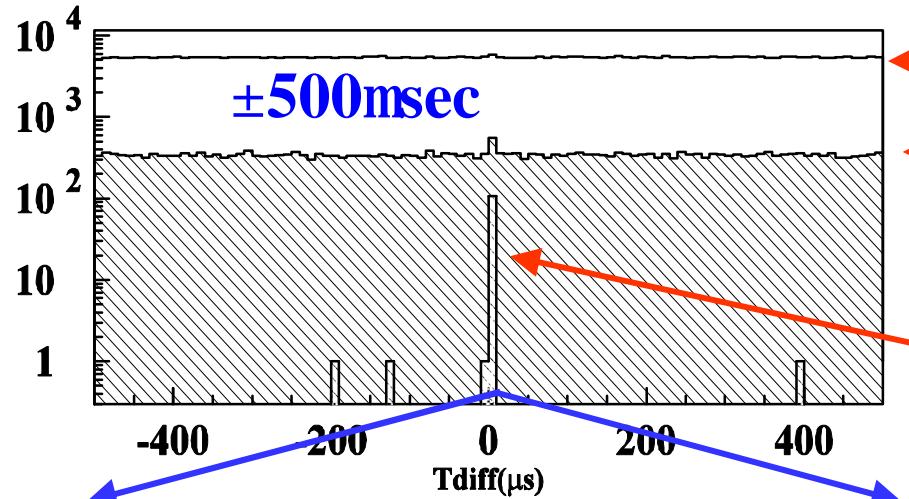
reconstructed neutrino energy



# n's from KEK



K2K-1+2 Jun1999 - Feb2004



Decay electron cut  
 ${}^320\text{MeV}$  Deposited Energy

No activity in Outer Detector (FV)  
 Event vertex in fiducial volume (FC)  
 More than 30MeV deposited energy

$$-0.2 < T_{SK} - T_{spill} - TOF < 1.3 \text{ msec}$$

(BG: 1.6 events within ±500ms  
 $2.4 \times 10^{-3}$  events in 1.5ms)

# Oscillation analysis

- Total number of FCFV events
- $E_n$  spectrum shape of FCFV 1-ring muon events
- Systematic error term

$$L(Dm^2, \sin 2q, f^x) = \\ L_{norm}(Dm^2, \sin 2q, f^x) \times L_{shape}(Dm^2, \sin 2q, f^x) \times L_{syst}(f^x)$$



Poisson probability  
for # FCFV events



Shape of  $E_n$  spectrum  
of 1-ring m events



Systematic error

$f^x$  - systematic error parameters

Normalization, Flux, and nQE/QE ratio are in  $f^x$

# Events at SK

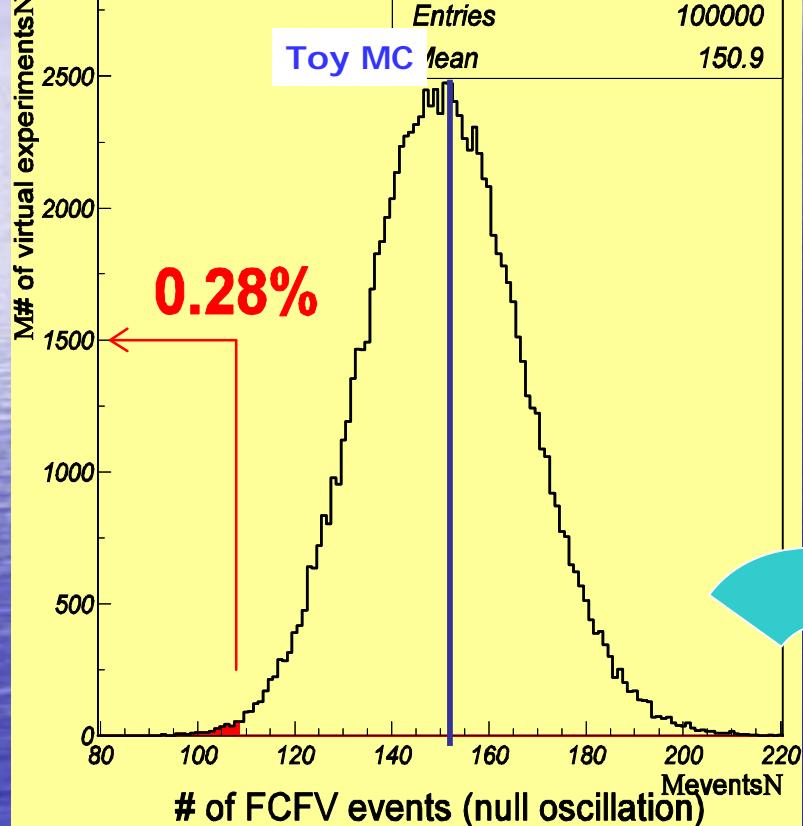
$$L_{norm}(\Delta m^2, \sin 2q, f^x)$$

$$L_{norm} = \frac{(N^{\exp})^{N^{\text{obs}}}}{N^{\text{obs}}!} \cdot \exp(-N^{\exp})$$

Fully contained events in  
22.5 kt fiducial volume of SK



107



107 150.9

$$N_{SK}^{\exp} = 107^{+12}_{-10}$$

$$N_{SK}^{\exp} = 151$$

SK Event summary		
	Data	MC
1-ring m-like	57	85.5
1-ring e-like	9	8.7
Multi-ring	40	56.7
Total	107	150.9

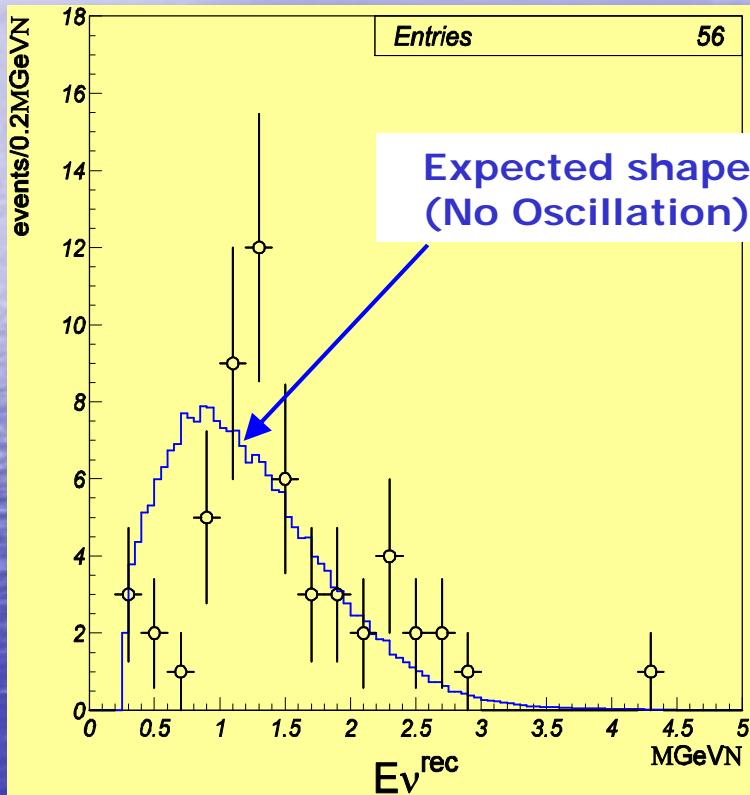
Only number of events

No oscillation probability = 0.28%

# Shape analysis

$$L_{shape}(\Delta m^2, \sin 2q, f^x)$$

CC-QE assumption



$$E_n^{rec} = \frac{(m_N - V)E_m - m_m^2/2 + m_N V - V^2/2}{(m_N - V) - E_m + p_m \cos q_m}$$

Only shape  
Kolmogorov-Smirnov test  
No oscillation probability = 0.74%

# Shape distortion

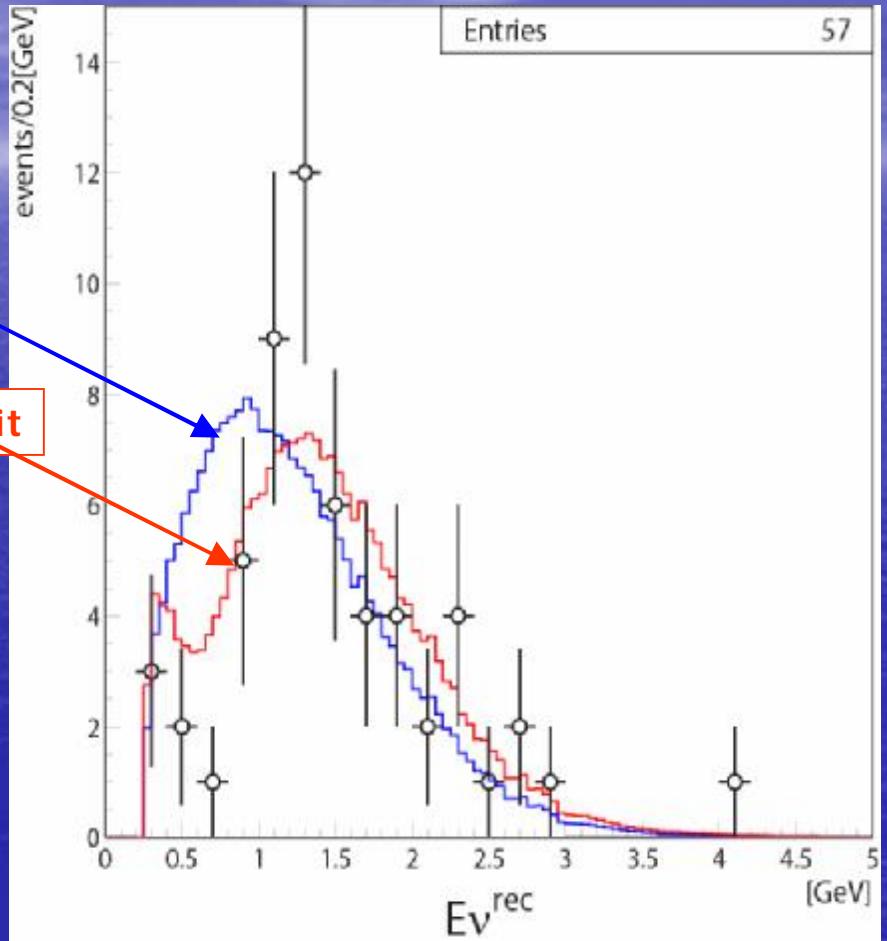
Expected shape  
(No Oscillation)

Best fit

Best fit value

$\sin^2 2\theta = 1.00$

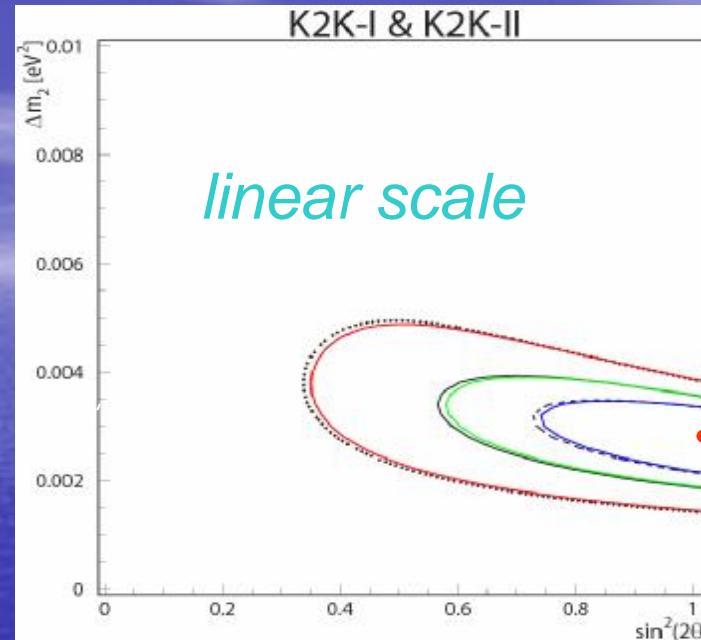
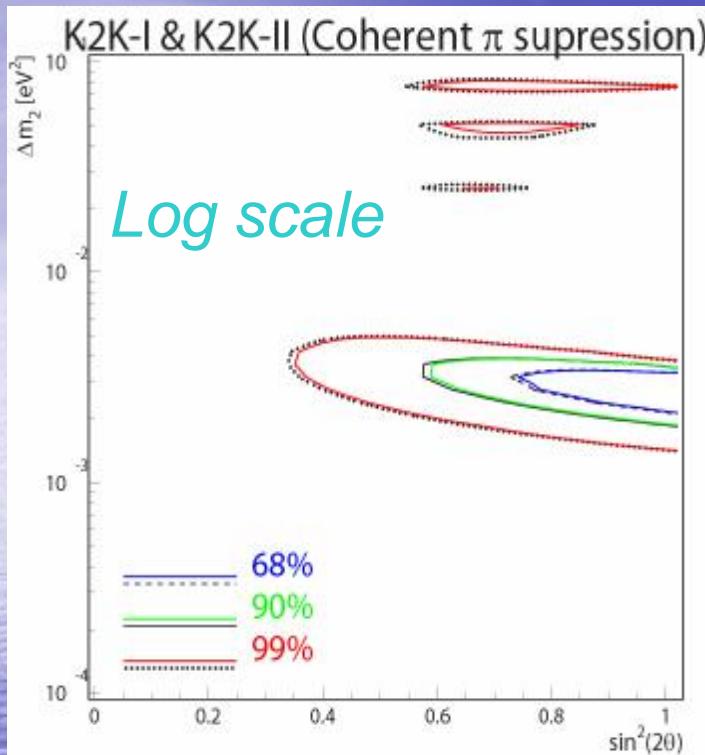
$\Delta m^2 [\text{eV}^2] = (2.79 \pm 0.36) \times 10^{-3}$



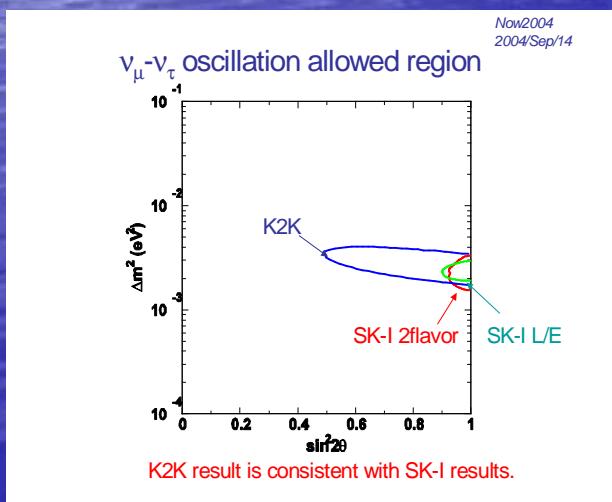
Kolmogorov-Smirnov test

Best fit probability = 36%

# Allowed region of oscillating parameters



Allowed region of  $\Delta m^2$  @  $\sin^2 2\theta = 1$   
 $1.99 \sim 3.33$  [eV<sup>2</sup>] (68%)  
 $1.9 \sim 3.6$  [eV<sup>2</sup>] (90%)



Null Oscillation probability  
0.0050% (4.06 $\sigma$ )

Evidence of  $\nu_\mu$  oscillation in K2K experiment

# Search for $n_m \xrightarrow{\text{R}} n_e$ oscillation

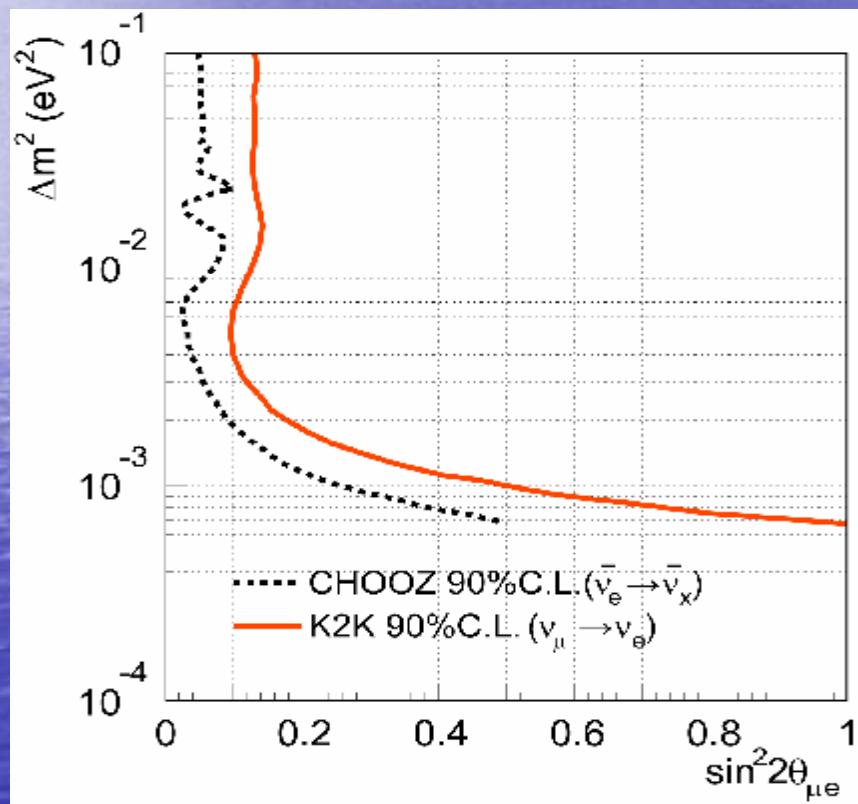
-K2K-1-	$\nu_\mu$ MC	beam $\nu_e$	Data
FCFV	81.1	0.81	55
Single ring	50.92	0.47	33
Electron like	2.66	0.40	3
Evis > 100 MeV	2.47	0.40	2
No decay-e	1.90	0.35	1
Pi0 cut	<b>0.58</b>	<b>0.17</b>	<b>0</b>

In total,  
#expected BG = 1.70  
#observed = 1

-K2K-2-	$\nu_\mu$ MC	beam $\nu$	Data
FCFV	77.4	0.86	57
Single ring	49.41	0.52	34
Electron like	3.21	0.44	5
Evis > 100 MeV	2.93	0.44	5
No decay-e	2.17	0.39	4
Pi0 cut	<b>0.74</b>	<b>0.21</b>	<b>1</b>

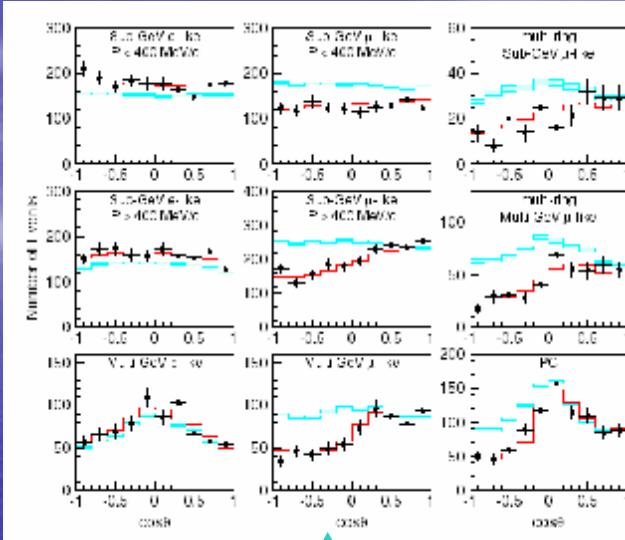
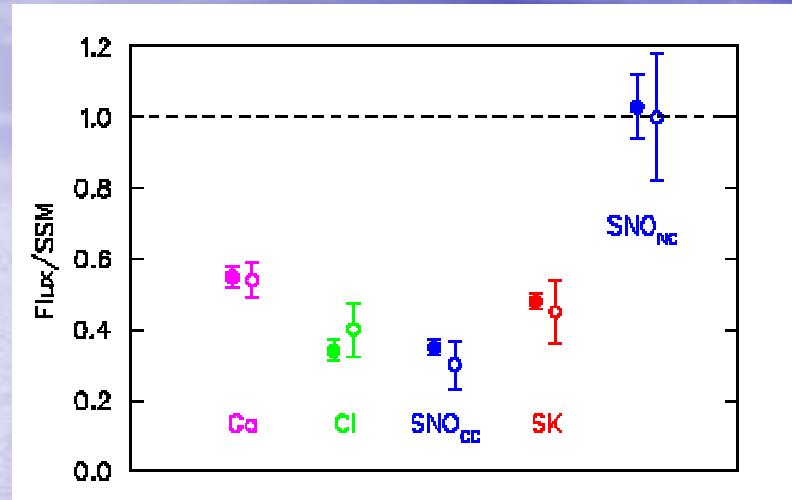
$n_m \rightarrow n_e$

$\Delta m^2$  vs.  $\sin^2 2\theta_{\mu e}$



Assumption:  $2\sin^2 2\theta_{\mu e} = \sin^2 2\theta_{13}$

# Evidence of neutrino oscillations



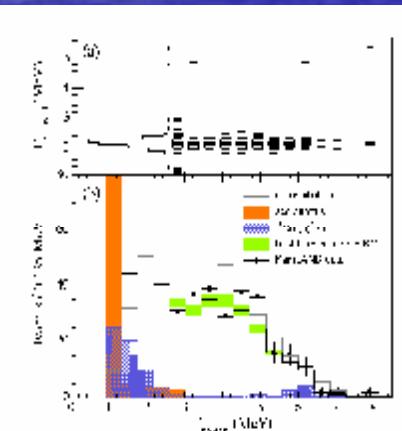
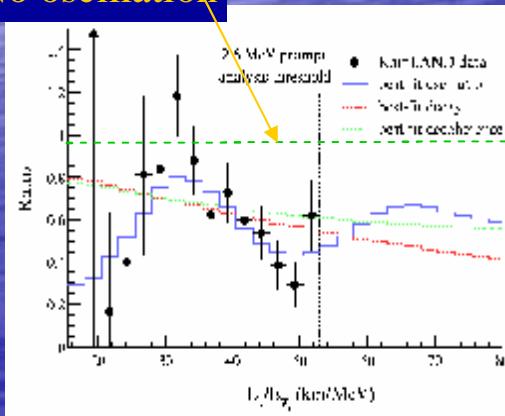
solar

$$\Delta m^2 \sim (7-8) \times 10^{-5} \text{ eV}^2$$

atmospheric

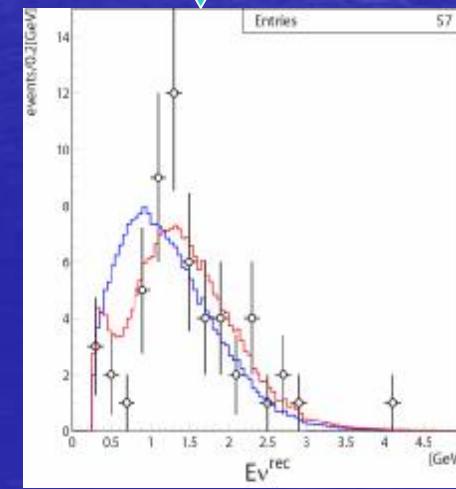
$$\Delta m^2 \sim (2-3) \times 10^{-3} \text{ eV}^2$$

No oscillation



Kamland

LSND  $\rightarrow \Delta m^2 = 0.2 - 10 \text{ eV}^2 \rightarrow m_n > 0.4 \text{ eV}$



# Neutrino masses and mixings

3 families

## Oscillation parameters

	central value	3s interval
$Dm^2_{12} (10^{-5} \text{ eV}^2)$	7.9	7.1 - 8.9
$Dm^2_{31} (10^{-3} \text{ eV}^2)$	2.2	1.4 - 3.3
$\sin^2 q_{12}$	0.31	0.24 - 0.40
$\sin^2 q_{23}$	0.50	0.34 - 0.68
$\sin^2 q_{13}$	0.0	<0.047

LSND  $\rightarrow Dm^2 = 0.2 - 10 \text{ eV}^2 \rightarrow m_n > 0.4 \text{ eV}$

Mixing	Quarks	Leptons
1-2 $q_{12}$	13°	33°
2-3 $q_{23}$	2.3°	45°
1-3 $q_{13}$	~ 0.5°	<13°

## Challenges in neutrino physics

LBL accelerator experiments

Tritium experiment

value of  $q_{13}$

CP violation in lepton sector

mass spectrum: normal or inverted

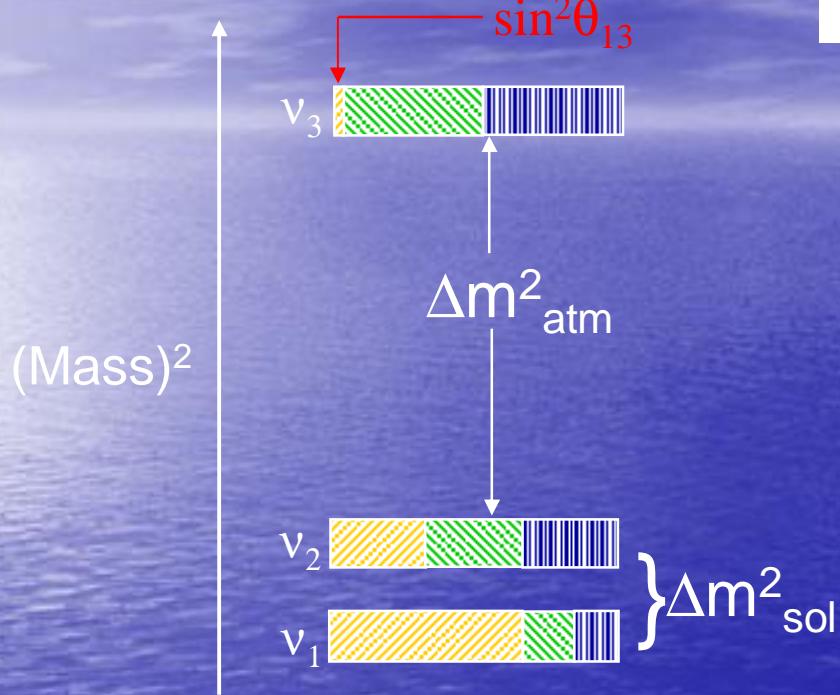
neutrino mass

Majorana/Dirac nature

reactor

Onbb

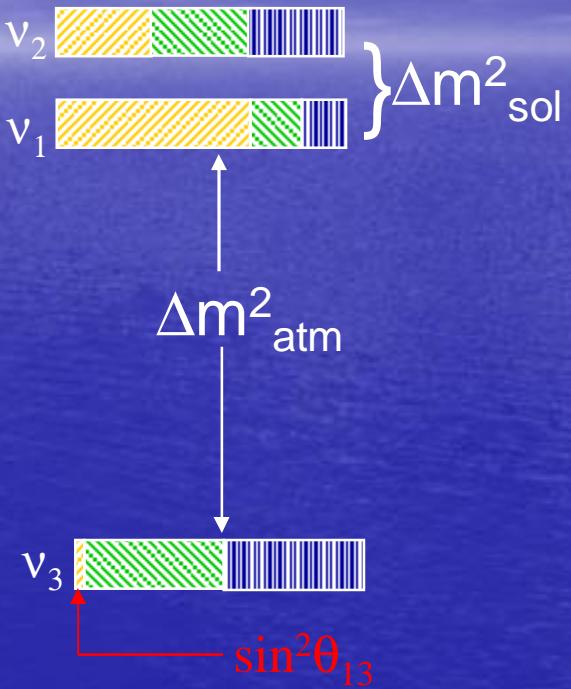
# Mass spectrum



Normal

$\sin^2 \theta_{13} = |\mathbf{U}_{e3}|^2 \rightarrow$  small  $\nu_e$  piece of  $\nu_3$   
 $\nu_3$  is at one end of  $\Delta m^2_{\text{atm}}$   
 We need an experiment with L/E sensitive to  $\Delta m^2_{\text{atm}}$   
 $(L/E \sim 500 \text{ km/GeV})$  involving  $\nu_e$

or



Inverted

$\nu_e [|\mathbf{U}_{ei}|^2]$

$\nu_\mu [|\mathbf{U}_{\mu i}|^2]$

$\nu_\tau [|\mathbf{U}_{\tau i}|^2]$

# Test of discrete symmetries

$$P(n_a \rightarrow n_b) \neq P(\bar{n}_b \rightarrow \bar{n}_a)$$

CPT violation

$$P(n_a \rightarrow n_a) \neq P(\bar{n}_a \rightarrow \bar{n}_a)$$

$$P(n_a \rightarrow n_b) \neq P(\bar{n}_a \rightarrow \bar{n}_b)$$

CP violation

$$P(n_a \rightarrow n_b) \neq P(\bar{n}_b \rightarrow \bar{n}_a)$$

T violation

$$A_{CP} = \frac{P(n_m \otimes n_e) - P(\bar{n}_m \otimes \bar{n}_e)}{P(n_m \otimes n_e) + P(\bar{n}_m \otimes \bar{n}_e)} @ \frac{Dm_{12}^2 L}{4E_n} \times \frac{\sin 2q_{12}}{\sin q_{13}} \times \sin d$$

For  $q_{12}=p/8$   $Dm_{12}^2=7 \times 10^{-5}$   $\sin^2 q_{12}=0.01$  (1/10 of CHOOZE limit)  $q = p/4$

$A_{CP} = 25\%$

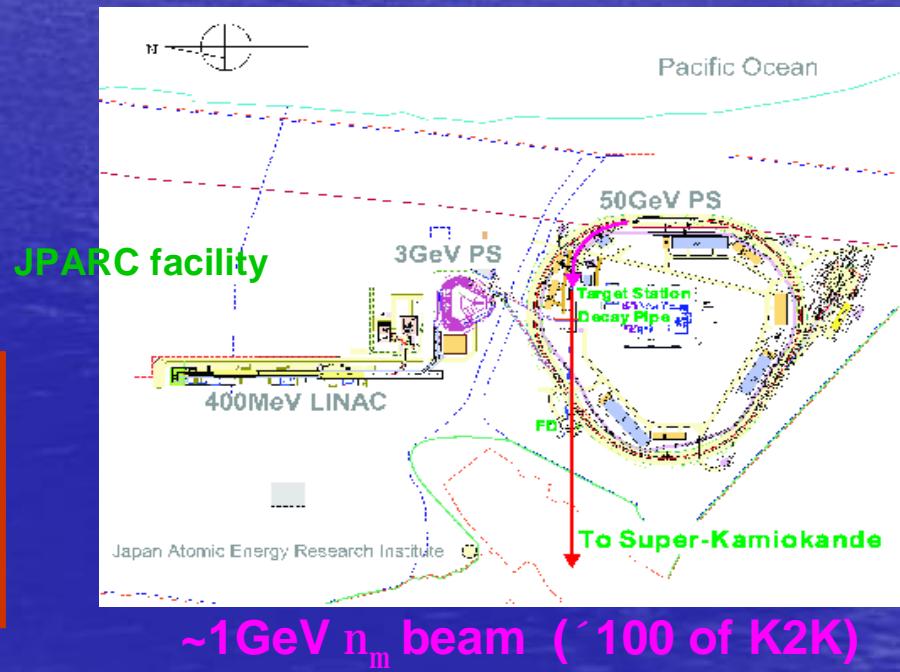
# LBL experiment T2K (Tokai to Kamioka)

12 countries, 60 institutions, ~180 collaborators

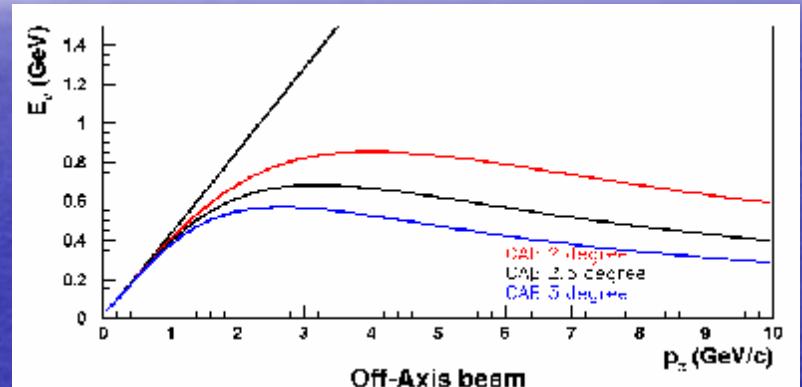
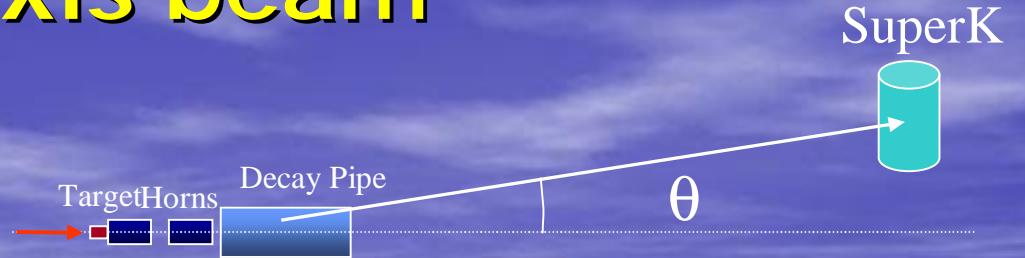
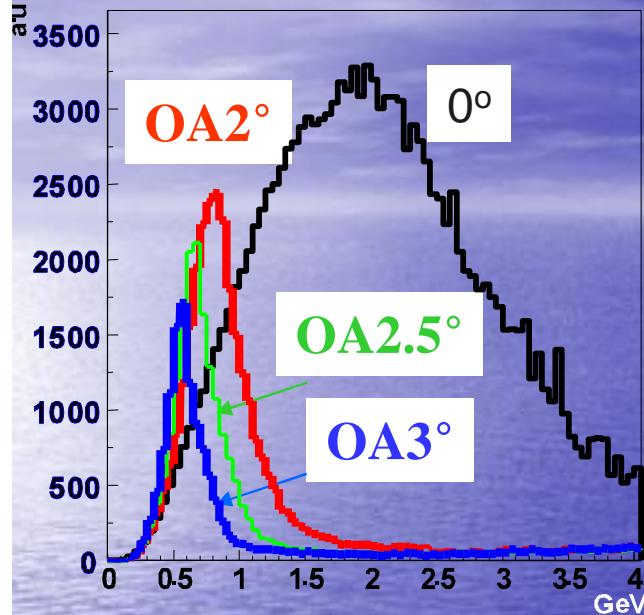


v beam      off-axis      on-axis

	JPARC	MINOS	K2K
E(GeV)	50	120	12
Int( $10^{12}$ ppp)	330	40	6
Rate (Hz)	0.29	0.53	0.45
Power (MW)	0.77	0.41	0.0052

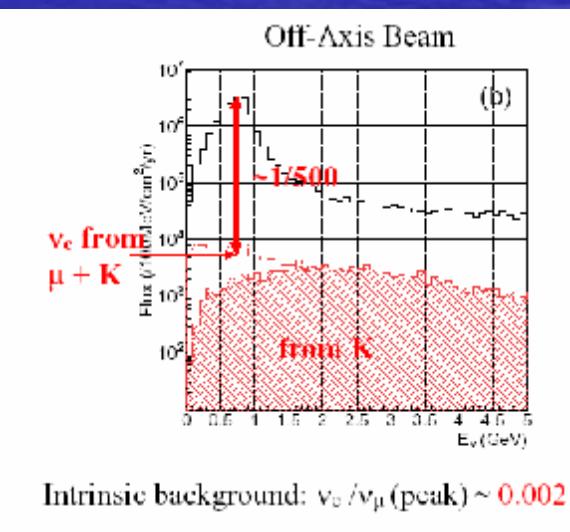


# Off-axis beam

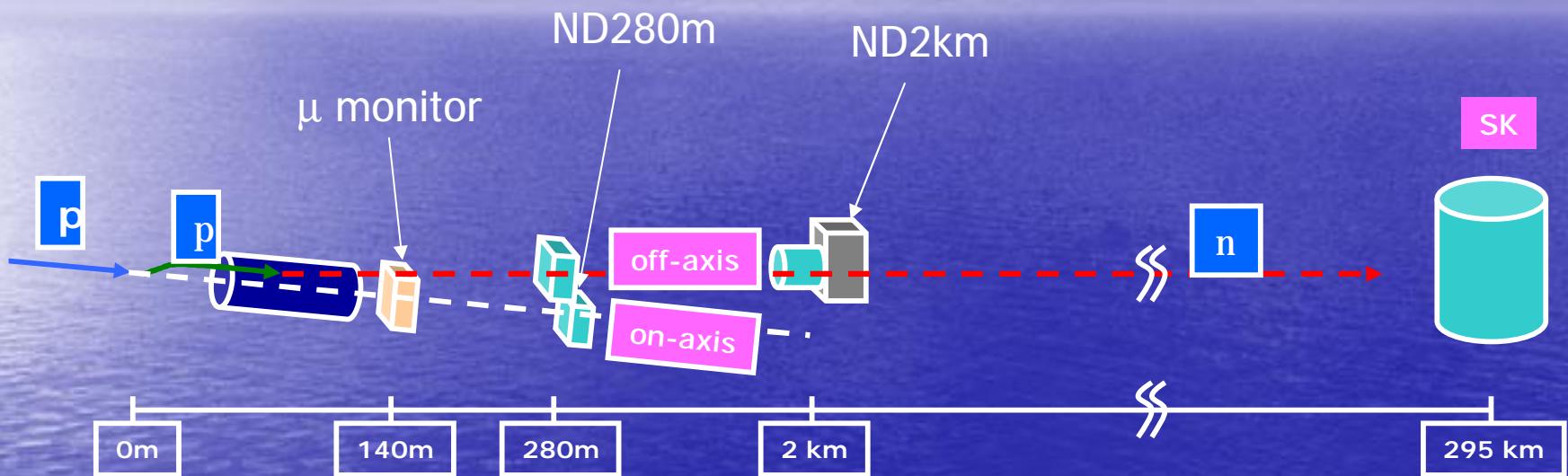


## Statistics at SK

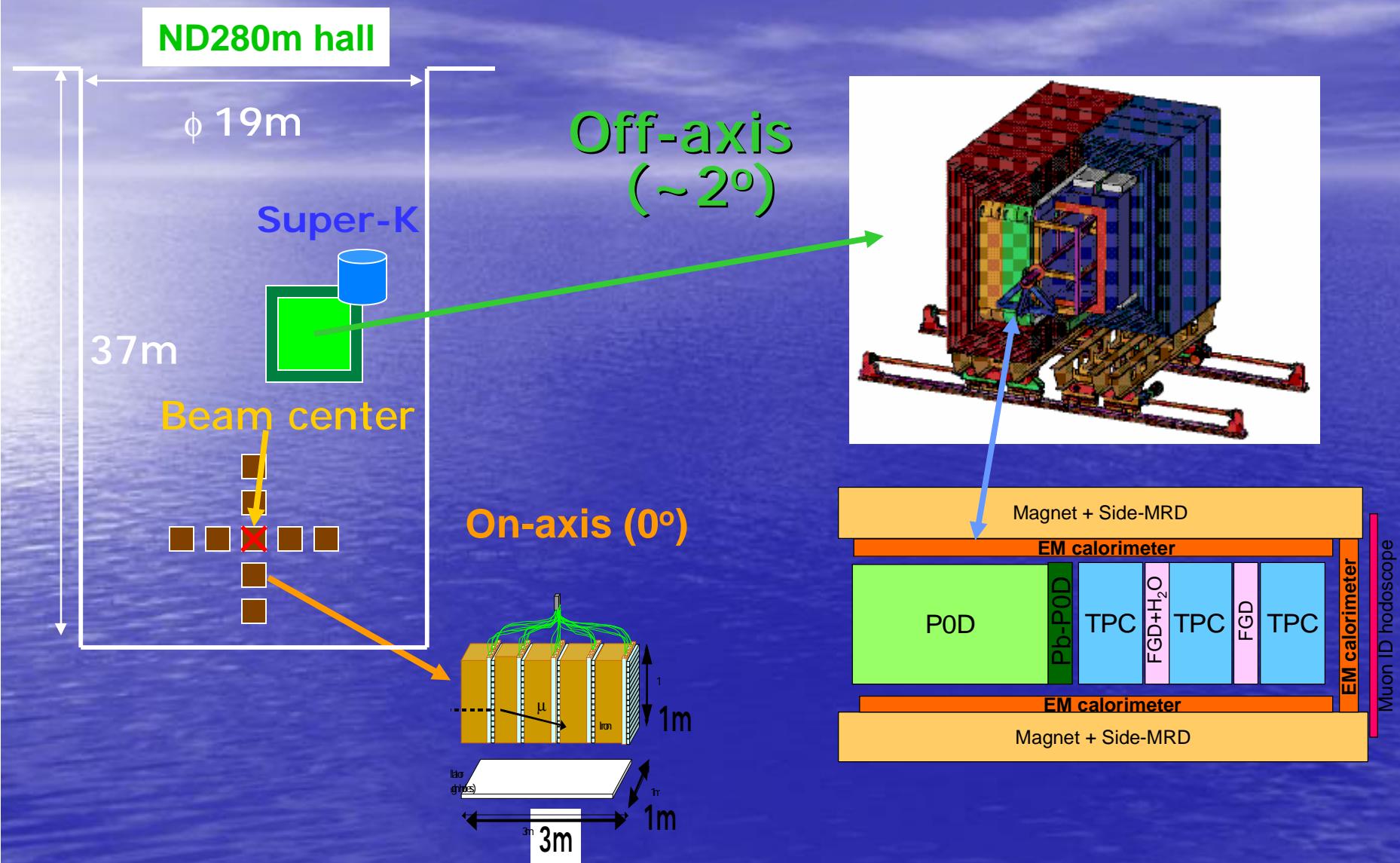
OAB 2.5 deg, 1 yr =  $10^{21}$  POT, 22.5 kt  
 $\sim 2200 n_m$  tot  
 $\sim 1600 n_m$  charged current  
 $n_e < 0.5\%$  at  $n_m$  peak



# T2K detectors

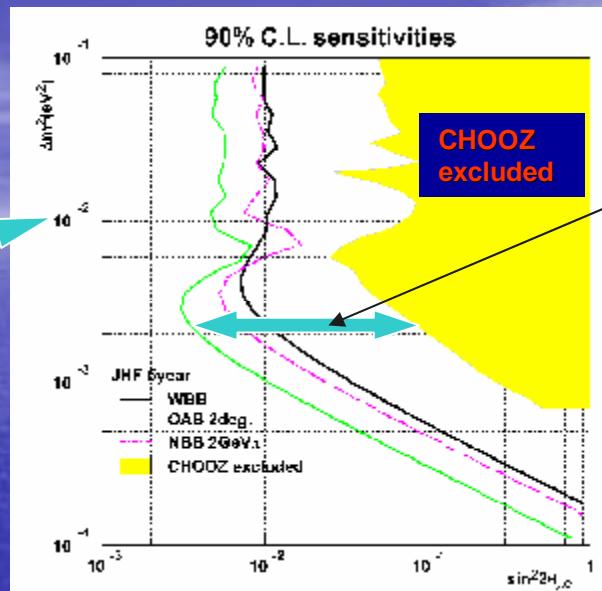
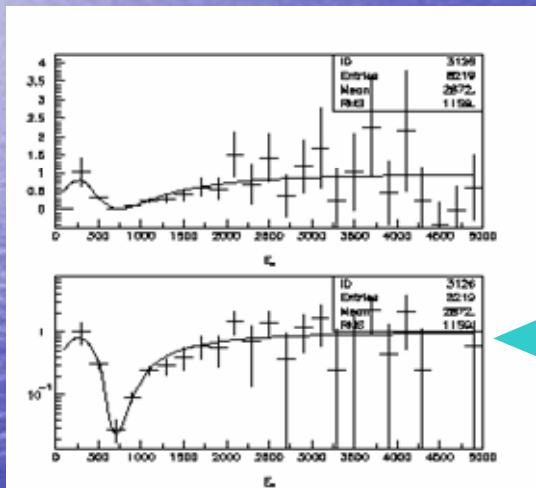


# Near Detectors at 280m



# Principle Goals of T2K

- Search for  $n_e$  appearance  
 $q_{13}$  sensitivity  $\pm 1^\circ$  (90% c.l.)



- Measurement  $Dm^2_{23}$  with accuracy of 1%  
 $d(\sin^2 2q_{23}) \sim 0.01$   
 $d(Dm^2_{23}) < 1 \cdot 10^{-4} \text{ eV}^2$

- Confirmation of  $n_m \leftrightarrow n_t$  oscillation

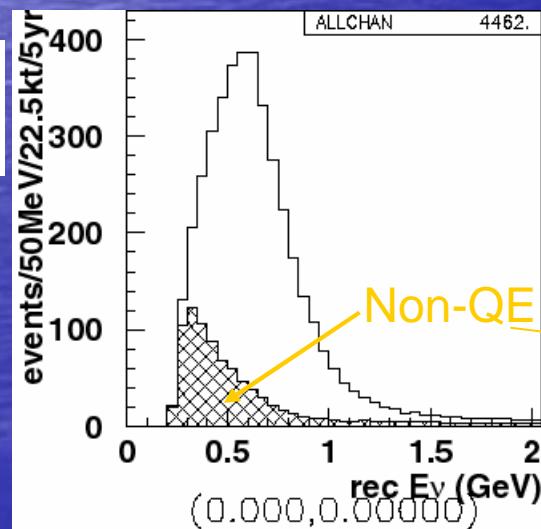
# Number of n events at SK for 5 years

Off-axis (deg)	w/o oscillation (events/22.5kt/5yr)	max. deficit	$\Delta m^2$ (eV <sup>2</sup> )
2.0	6683	1724	$3.22 \times 10^{-3}$
2.5	4462	1103	$2.70 \times 10^{-3}$
3.0	3006	752	$2.33 \times 10^{-3}$

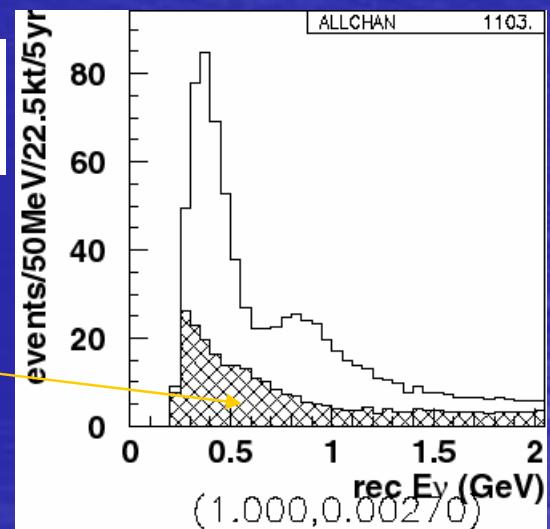
$(\sin^2 2\theta=1)$

Reconstructed  $E_\nu$  spectrum at SK (OA2.5deg)

no  
oscillation



$(\sin^2 2\theta, \Delta m^2)$   
 $= (1.0, 0.0027)$



# LBL experiments

2006 -08

MINOS (FNAL)

$n_m \rightarrow n_m$  search for  $n_m \rightarrow n_e$

OPERA (CERN/Gran Sasso)

search for  $n_m \rightarrow n_t$  appearance

MiniBooNe(FNAL)

LSND anomaly

2009....

T2K Phase I

search for  $n_m \rightarrow n_e$  appearance/ $q_{13}$  measurement

Phase II depends on  $q_{13}$

CP – violation, if  $q_{13} \neq 0$

NOVA (FNAL)

CP – violation, mass hierarchy

# Summary

- Neutrinos have masses
- Clear signal of New Physics beyond the Standard Model  
(Solar, atmospheric, accelerator experiments)
- Exciting physics from  
running and future long base-line experiments
  - search/measurement of  $q_{13}$   $|U_{e3}| = ?$
  - precision measurements of  $\theta_{23}$  and  $\Delta m^2_{23}$
  - CP violation if  $\theta_{13}$  is large
  - mass hierarchy
- Unexpected or exotic properties?