

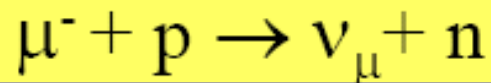
**ПРЕЦИЗИОННОЕ ИЗМЕРЕНИЕ СКОРОСТИ ЗАХВАТА МЮОНА  
В ВОДОРОДЕ И ОПРЕДЕЛЕНИЕ ПСЕВДОСКАЛЯРНОГО  
ФОРМ ФАКТОРА ПРОТОНА  $g_p$**

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# Precision Measurement of Muon Capture on the Proton

## *“ $\mu$ Cap experiment”*



[www.npl.uiuc.edu/exp/mucapture/](http://www.npl.uiuc.edu/exp/mucapture/)

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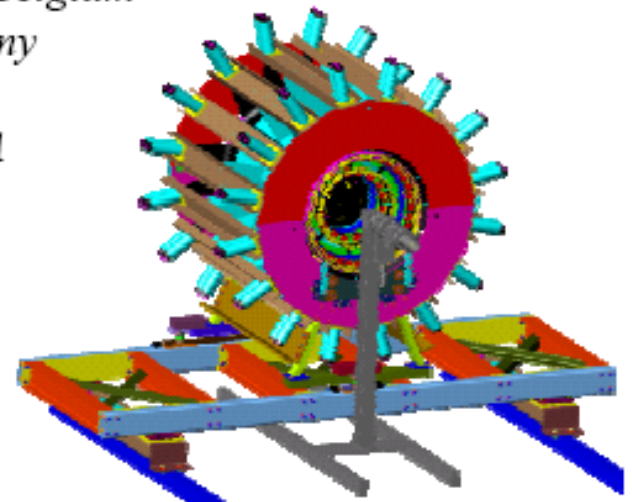
*University of Illinois, Urbana-Champaign, USA*

*Universite Catholique de Louvain, Belgium*

*TU Munich, Garching, Germany*

*Boston University, USA*

*University of Kentucky, USA*



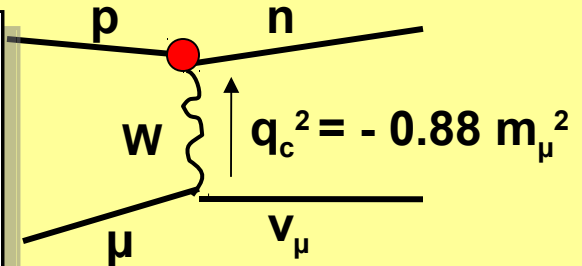
# Muon Capture on Proton



MuCap goal: to measure  $\mu p$ -capture rate  $\Lambda_s$  with 1% (or better) precision

$$V_\alpha = g_V(q^2) \gamma_\alpha + \frac{i g_M(q^2)}{2 M_N} \sigma_{\alpha\beta} q^\beta$$

$$A_\alpha = g_A(q^2) \gamma_\alpha \gamma_5 + \frac{\mathbf{g}P(q^2)}{m_\mu} q_\alpha \gamma_5$$



**$\mu p$ -capture offers a unique probe of the nucleon's electroweak axial structure**

# Muon capture on proton

$$V_{\alpha} = g_V(q^2) \gamma_{\alpha} + \frac{i g_M(q^2)}{2 M_N} \sigma_{\alpha\beta} q^{\beta}$$

$$A_{\alpha} = g_A(q^2) \gamma_{\alpha} \gamma_5 + \frac{\mathbf{gP}(q^2)}{m_{\mu}} q_{\alpha} \gamma_5$$

## Стандартная Модель и структура нуклонов

$$g_v = 0.9755 \pm 0.0005$$

$$g_a = 1.245 \pm 0.003$$

$$g_m = 3.582 \pm 0.003$$

$$g_p(\text{th}) = 8.26 \pm 0.23$$

$$g_p(\text{OMC}) = 6 - 12$$

$$g_p(\text{RMC}) = 12.2 \pm 0.9 \pm 0.4$$

# pseudoscalar form factor $g_p$

PCAC:

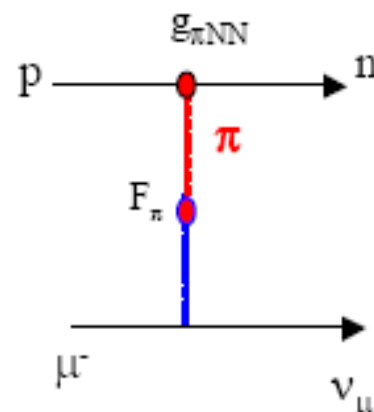
$$g_P(q^2) = \frac{2m_\mu M}{m_\pi^2 - q^2} g_A(0)$$

$$g_p = 8.7$$

heavy baryon chiral perturbation theory:

$$g_P(q^2) = \frac{2m_\mu g_{\pi NN} F_\pi}{m_\pi^2 - q^2} - \frac{1}{3} g_A(0) m_\mu M r_A^2$$

$$g_p = (8.74 \pm 0.23) - (0.48 \pm 0.02) = 8.26 \pm 0.23$$



$\Lambda$  calculations  $O(p^3)$  show good convergence: 100 % 25 % 3 %  
 delta effect small LO NLO NNLO

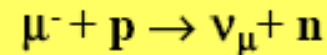
$g_{\pi NN}$   
 13.31(34)  
 13.0(1)  
 13.05(8)

author	year	$g_p$	$\Lambda_S$	$\Lambda_T$	comment
Primakoff	1959		664(20)	11.9(7)	smaller $g_A$
Opat	1964		634	13.3	smaller $g_A$
Bernard et al	1994	8.44(23)			
Fearing et al	1997	8.21(9)			
Govaerts et al	2000	8.475(76)	688.4(38)	12.01(12)	
Bernard et al	2000/1		687.4 (711*)	12.9	NNLO, small scale
Ando et al	2001		695 (722*)	11.9	NNLO

\*NLO result

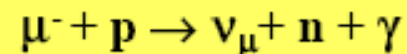
## Experimental information on $g_p$

### Ordinary Muon Capture



BR $\sim 10^{-3}$ , 8 experiments 1962-82, BC, neutron, electron detection  
*“in principle”* most direct  $g_p$  measurement

### Radiative Muon Capture



BR $\sim 10^{-8}$ , TRIUMF (1998),  $E_\gamma > 60$  MeV,  $297 \pm 26$  events  
closer to pion pole  $\rightarrow$  *3x sensitivity of OMC*  
*theory more involved* (min substitution, ChPT)

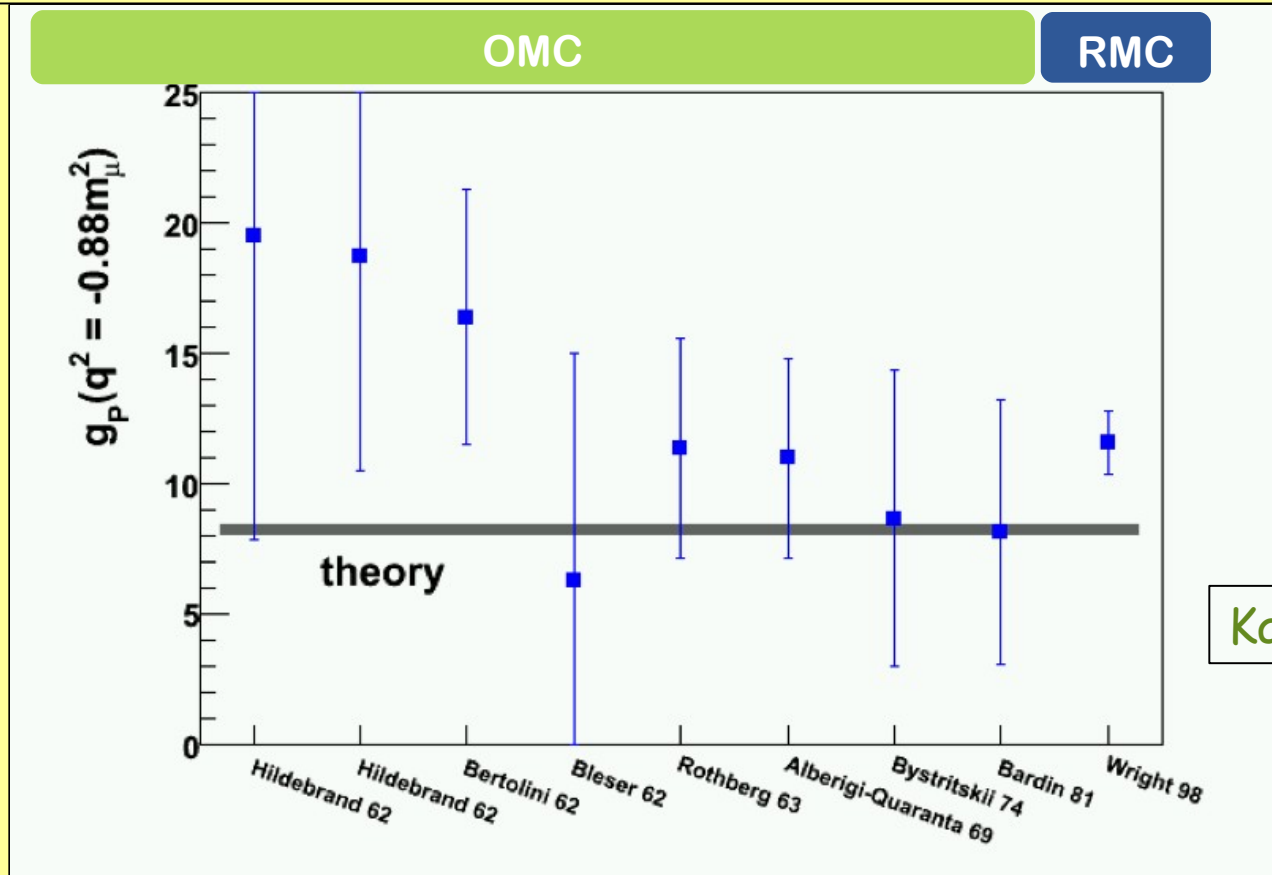
- Muon capture in nuclei

$\mu + {}^3\text{He} \rightarrow \nu + {}^3\text{H}$   $\Lambda_{st} = 1496 \pm 4 \text{ s}^{-1}$  PSI (1998)  
 $g_p = g_p^{\text{th}}$  ( $1.08 \pm 0.19$ ) error dominated by 3-N theory  
correlation measurements

- $\pi$  electro production at threshold

# 50 years of effort to determine $g_P$

$$\lambda + \underline{g} + \frac{1}{\epsilon^2} d + \dots$$



Kammel&Kubodera

“ Radiative muon capture in hydrogen was carried out only recently with the result that the derived  $g_P$  was almost 50% too high. If this result is correct, it would be a sign of new physics... ”

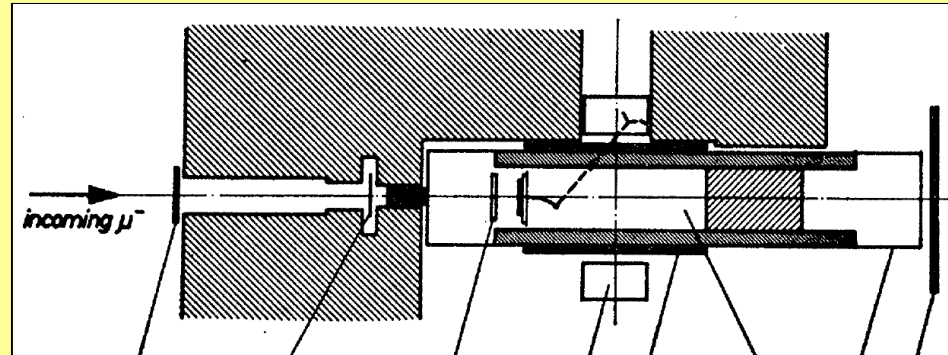
— Lincoln Wolfenstein (*Ann.ReNucl.Part.Sci.* 2003)



# Pioneers of muon capture experiments



Emilio Zavattini 1927-2007



1969 Bologna-Pisa-CERN

H<sub>2</sub> –target 8 atm

$$g_p = 11.0 \pm 3.8$$



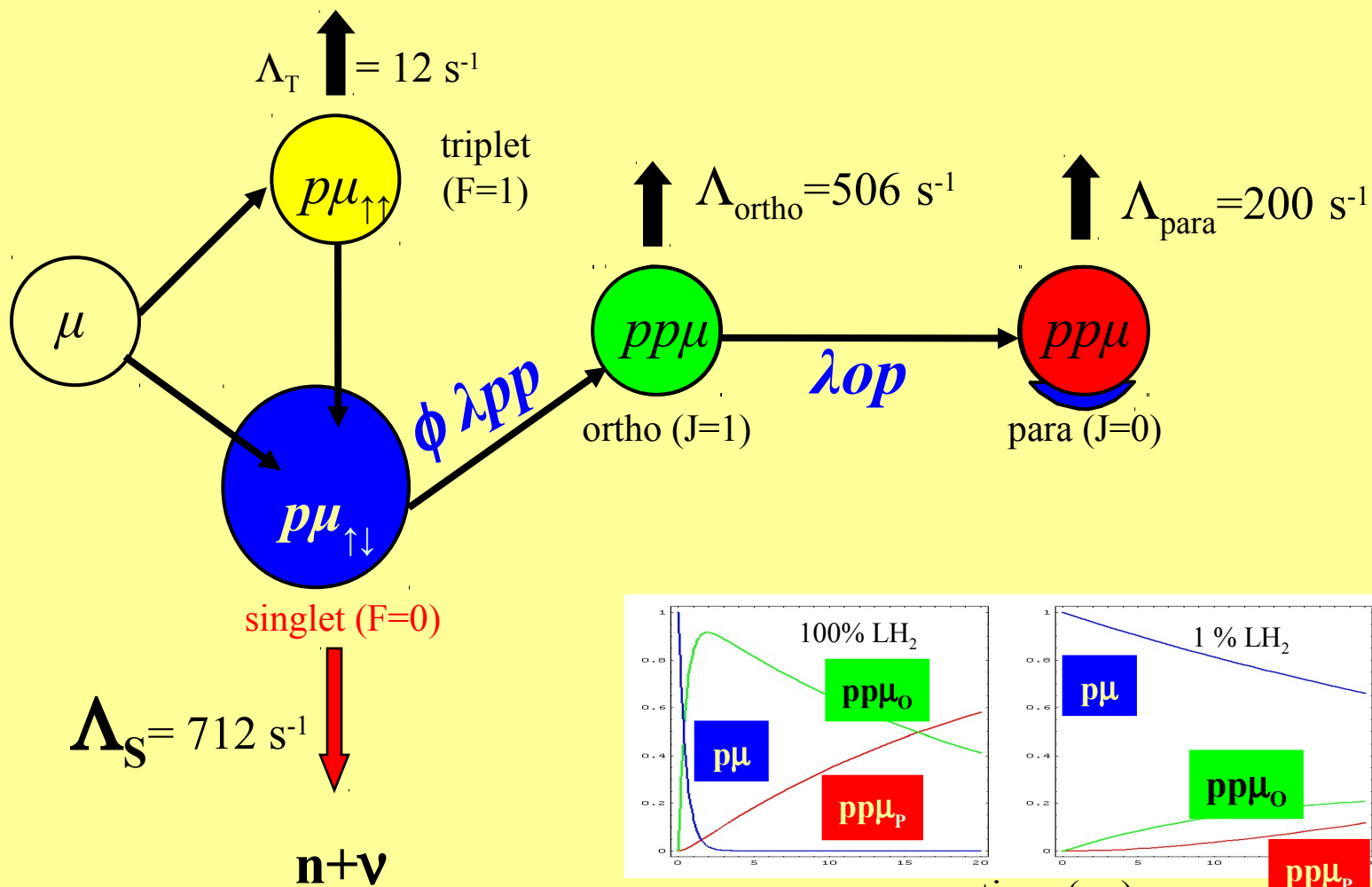
1973 Dubna group

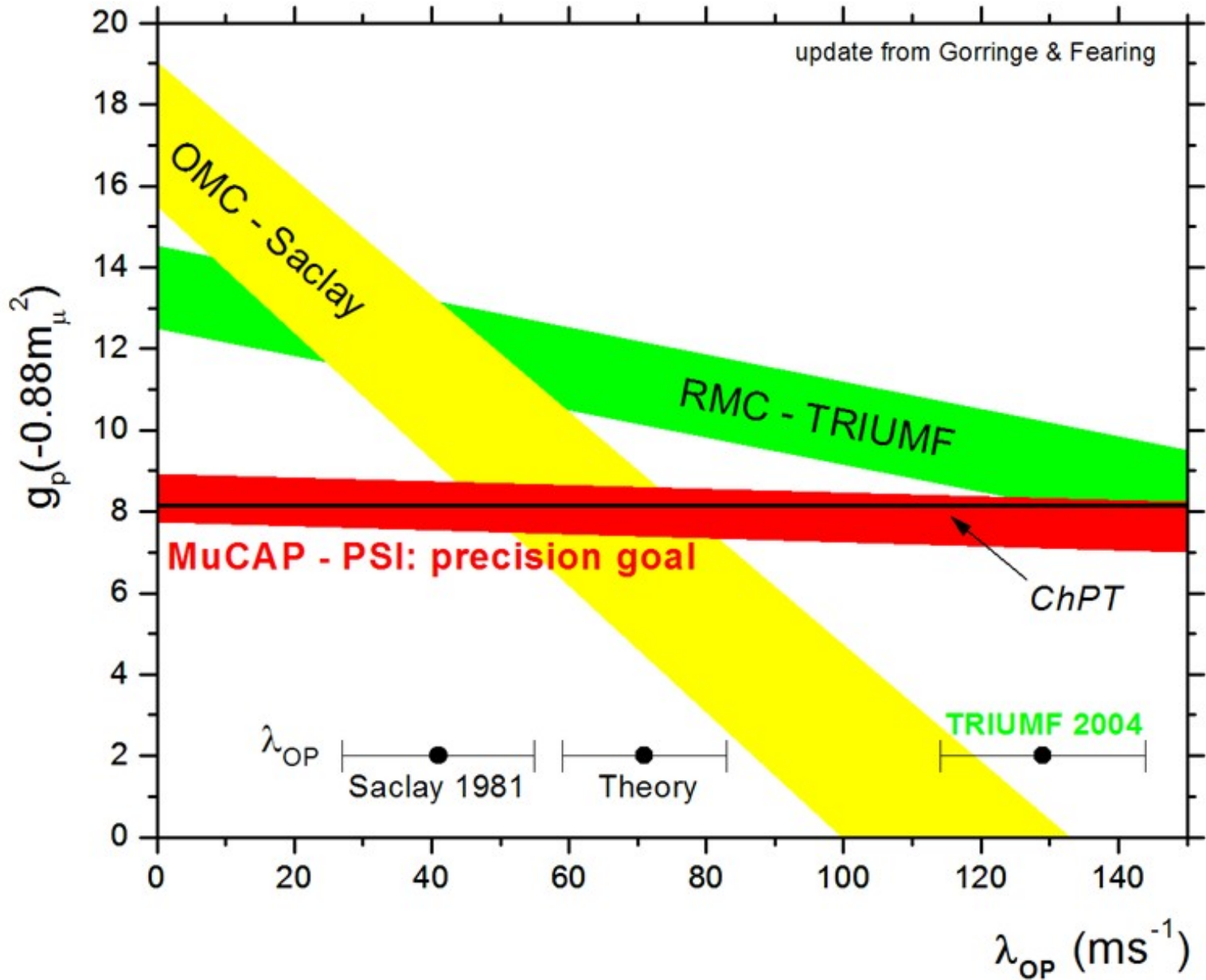
H<sub>2</sub> –target 41 atm

$$g_p = 8.7 \pm 5.7$$

Expt. Problems

- Wall effects
- Background
- Neutron detection efficiency





# Стратегия MuCap эксперимента

## Измерение времени жизни ( $\tau$ )

с точностью **10ppm**, регистрация  $\mu \rightarrow e\nu\nu$  распадов ( $10^{10}$ )

## Однозначность интерпретации

захват из  $F=0$  состояния  $\mu p$  атома при плотности  $1\% \text{ H}_2$

## Использование методики активной мишени (TPC)

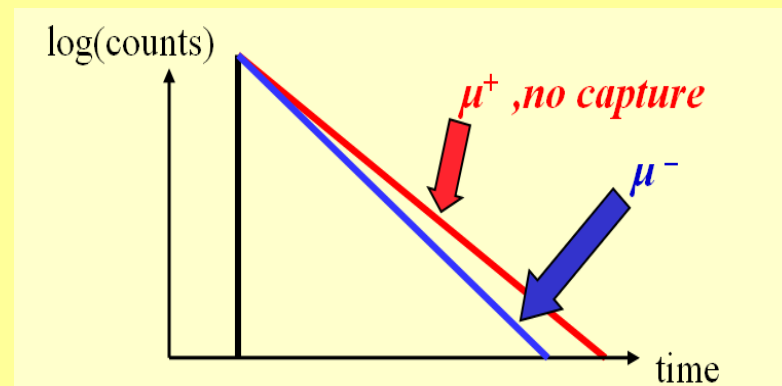
с точной регистрацией координат и времени остановок мюонов, реконструкция треков электронов к точке распада.

## Использование ультрачистого водорода $C_z < 10\text{ppb}$

## Контроль примесей по реакциям: $\mu p + Z \rightarrow \mu Z + p$ , $C_z \sim 10\text{ppb}$ .

## Обеспечение изотопической чистоты водорода

$\mu p + d \rightarrow \mu d + p + 134\text{eV}$ , примесь  $Cd < 1\text{ppm}$ , диффузия  $\mu d \sim \text{cm}$



# PSI meson factory

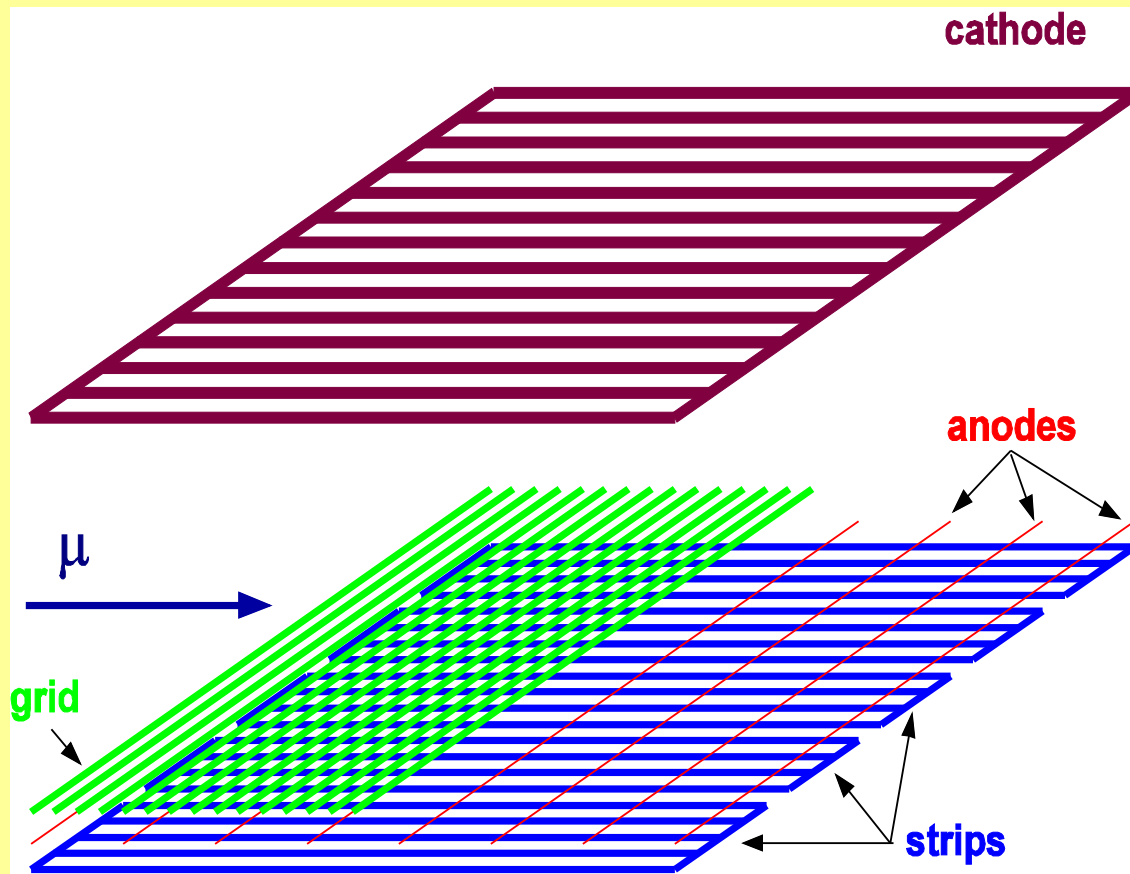


600MeV protons  
2mA extracted proton beam  
100% duty factor  
High intensity muon channels  
Muon-on-request mode

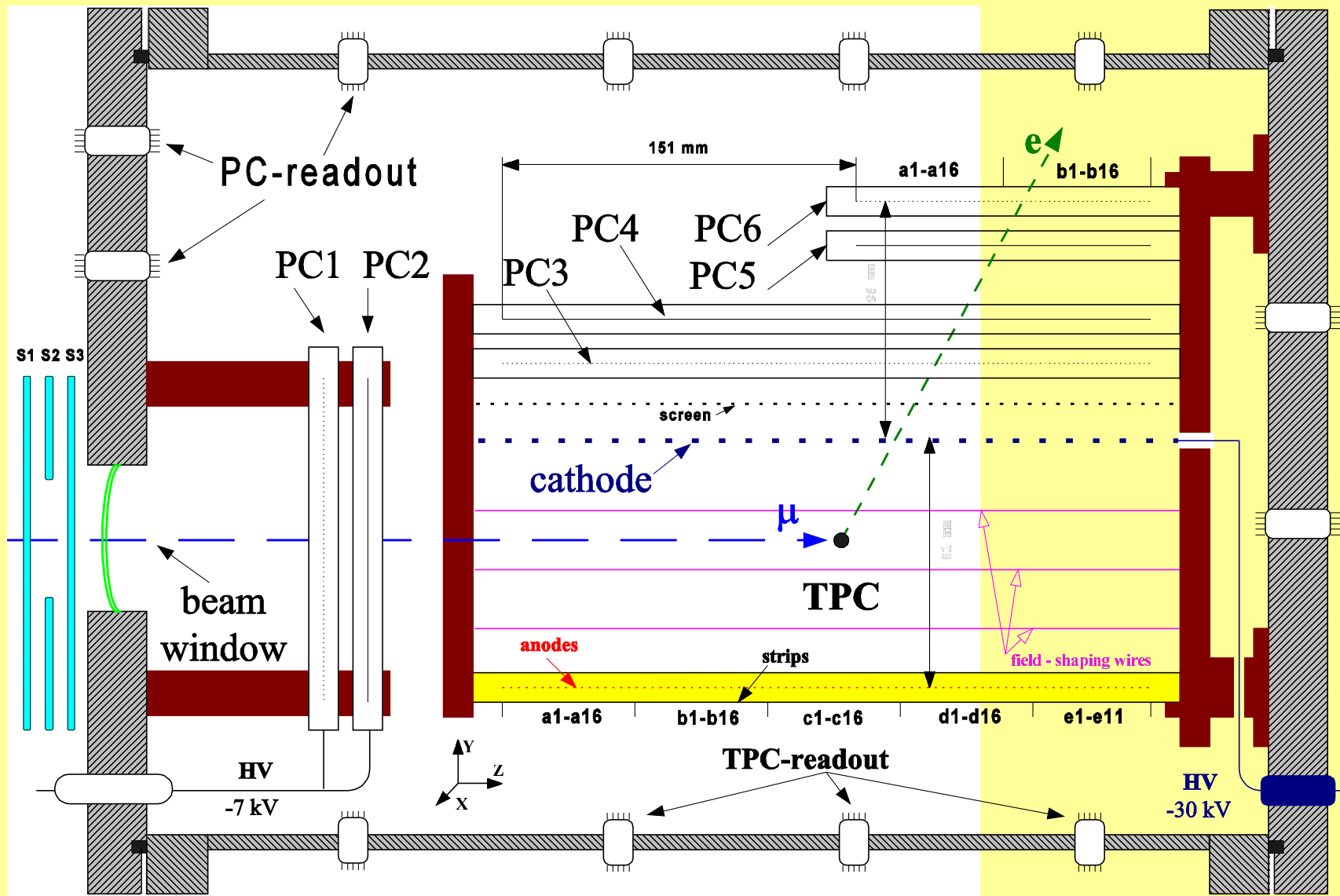
PNPI in PSI since 1986

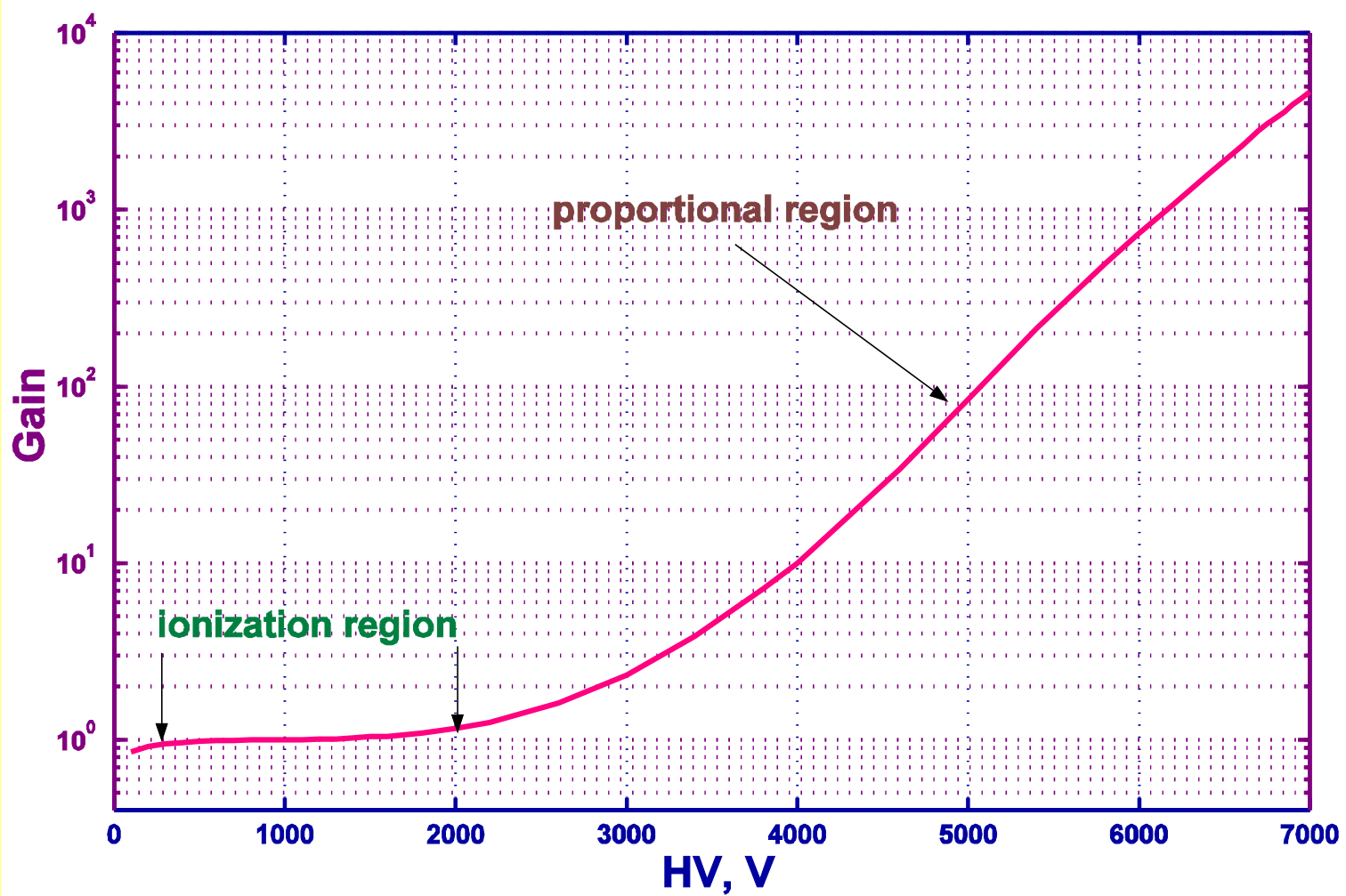
- **Muon catalyzed dd-and dt-fusion experiments** ( completed )
- **Muon capture on He-3** ( completed )
- **Muon capture on proton** ( completed )
- **Muon capture on deuteron** ( in progress )

## Schematic view of the TPC

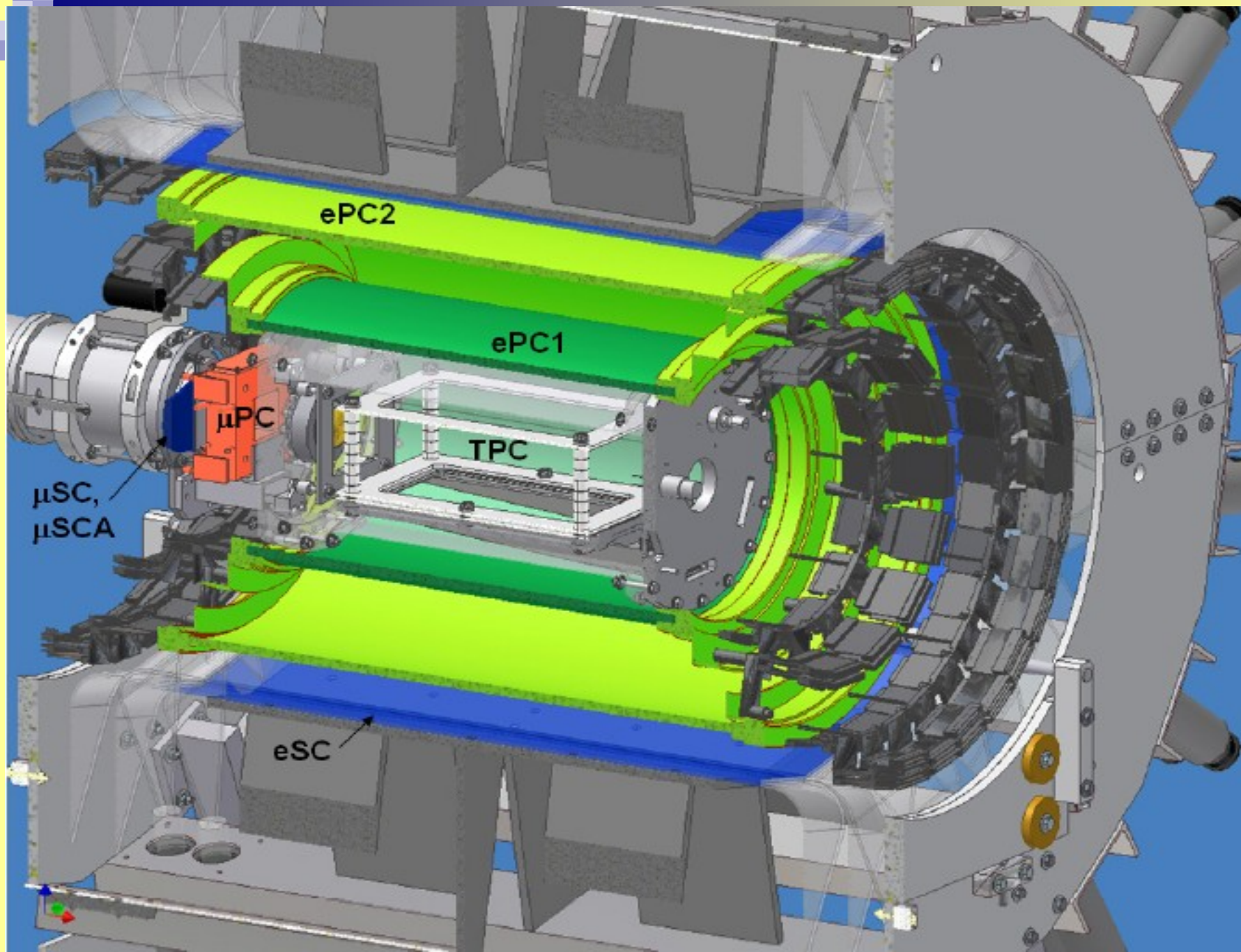


***The trajectories of charged particles are measured in 3D space with resolution (rms) 1-2 mm.***

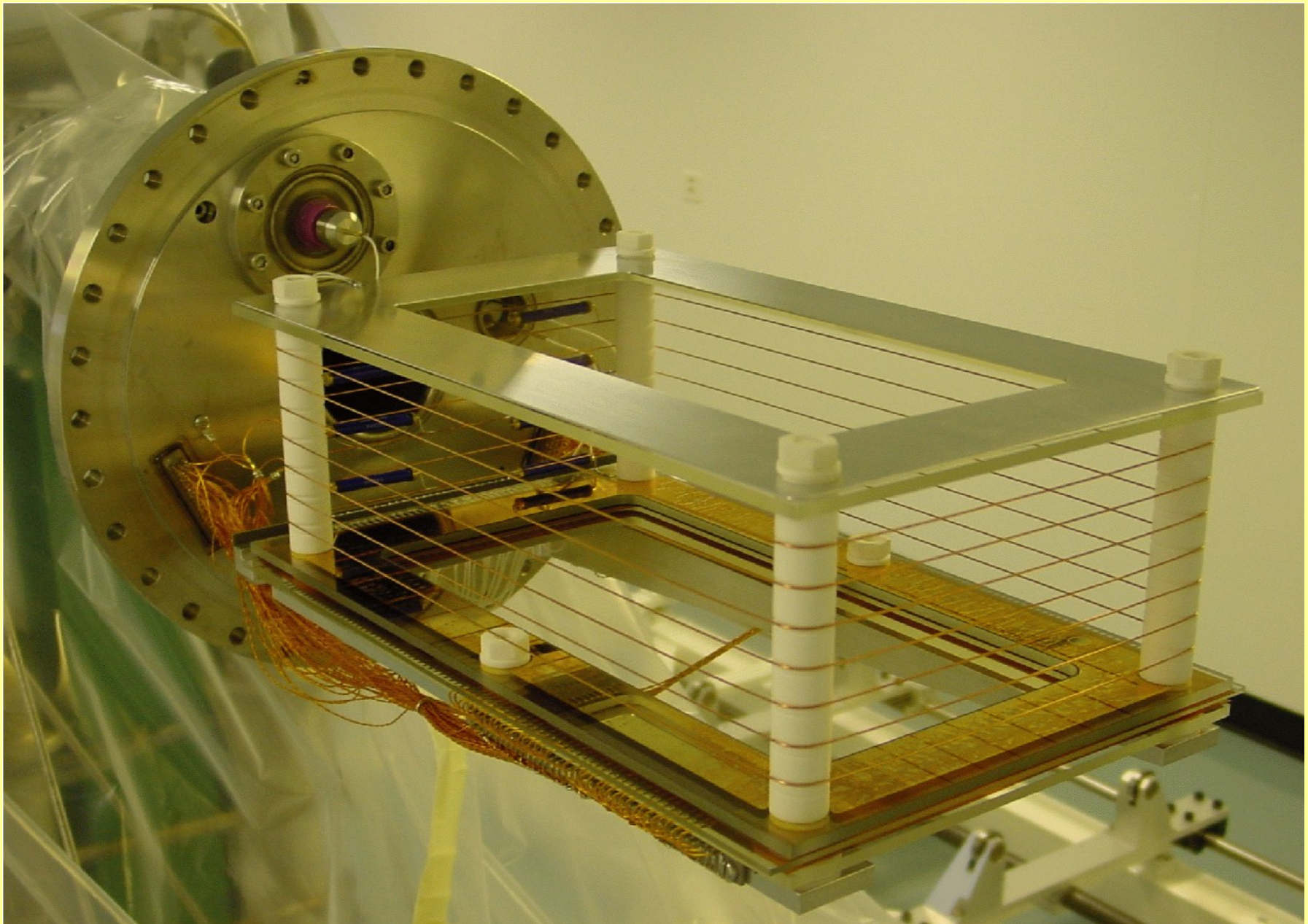




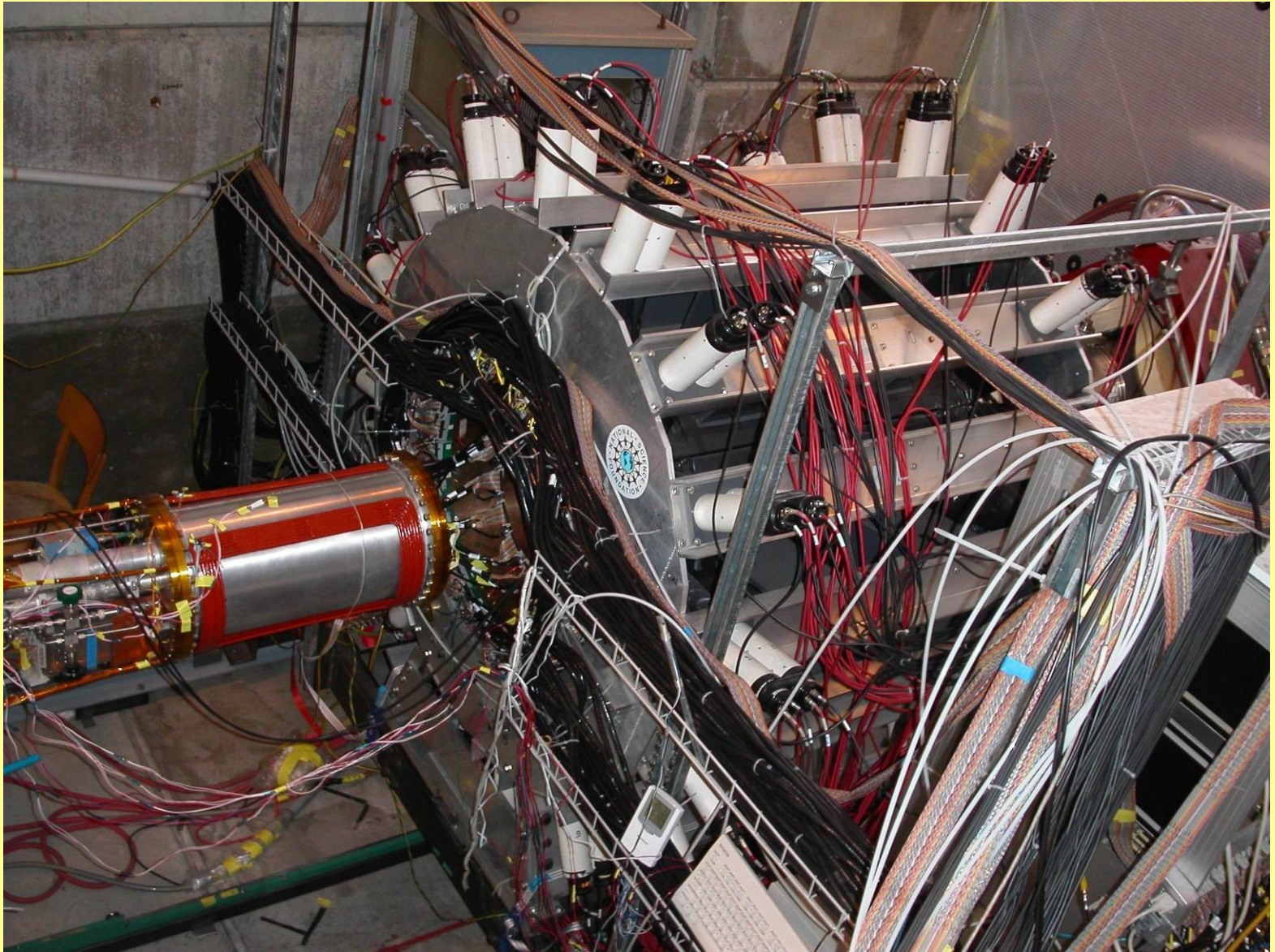


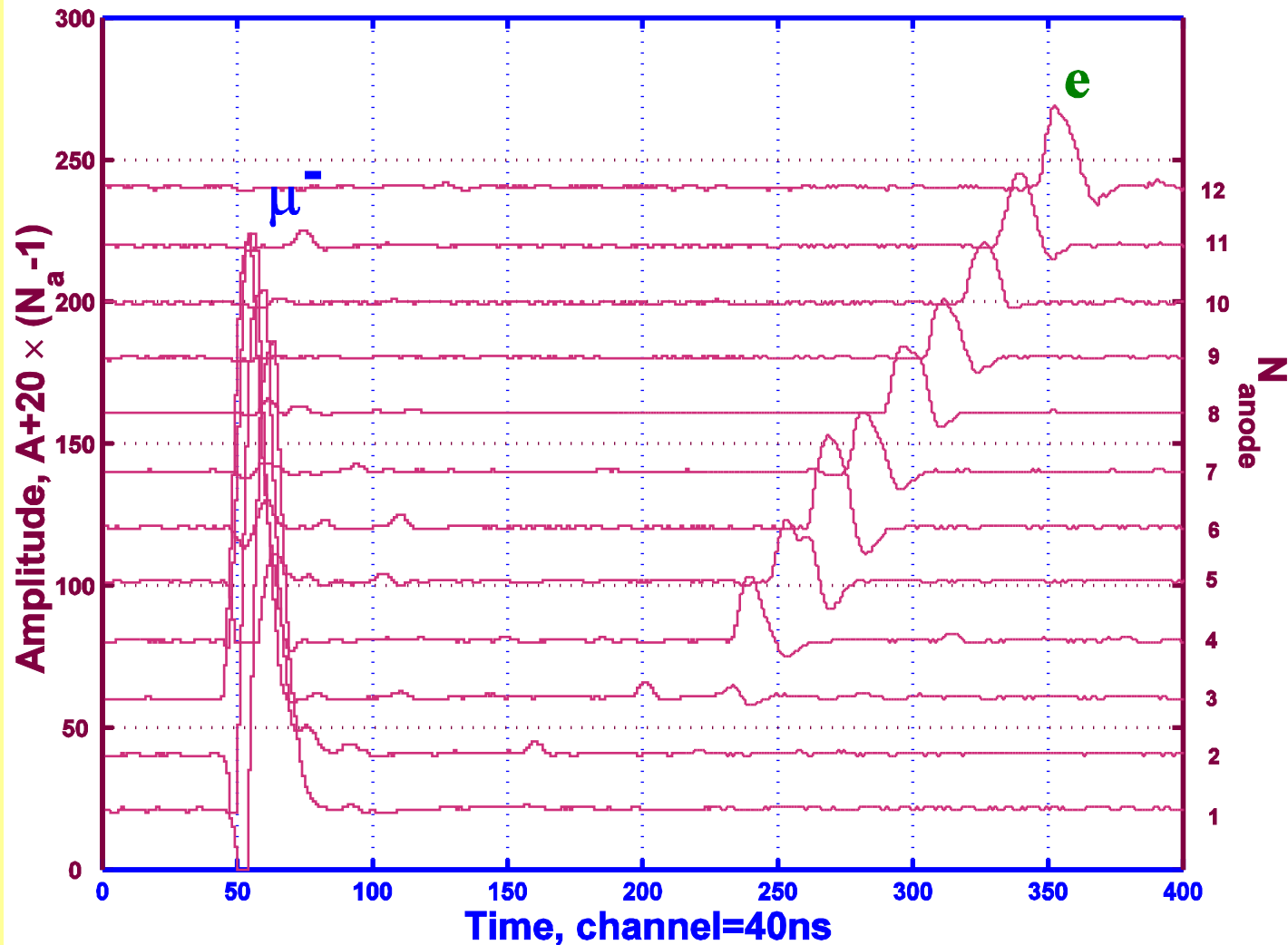




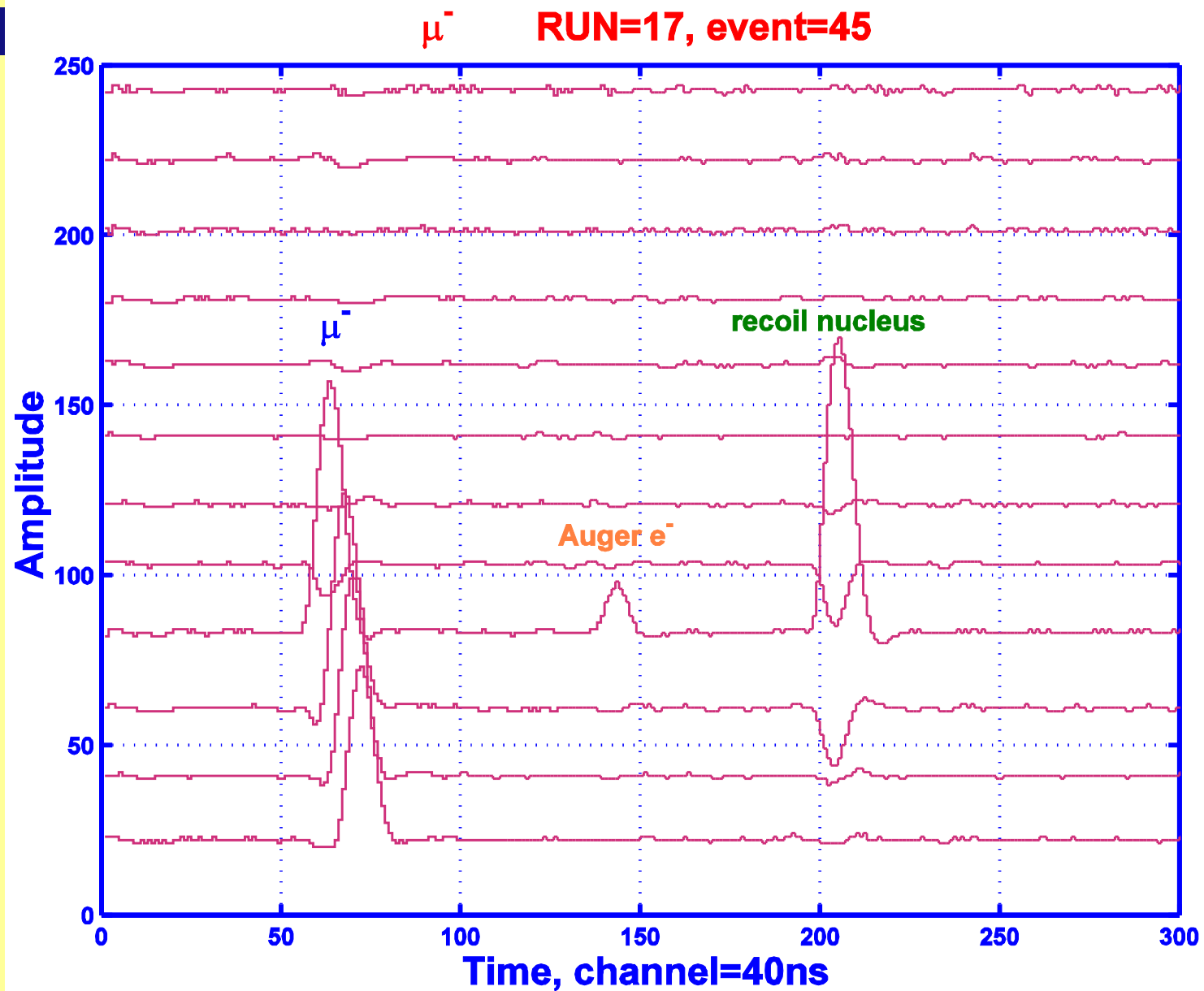






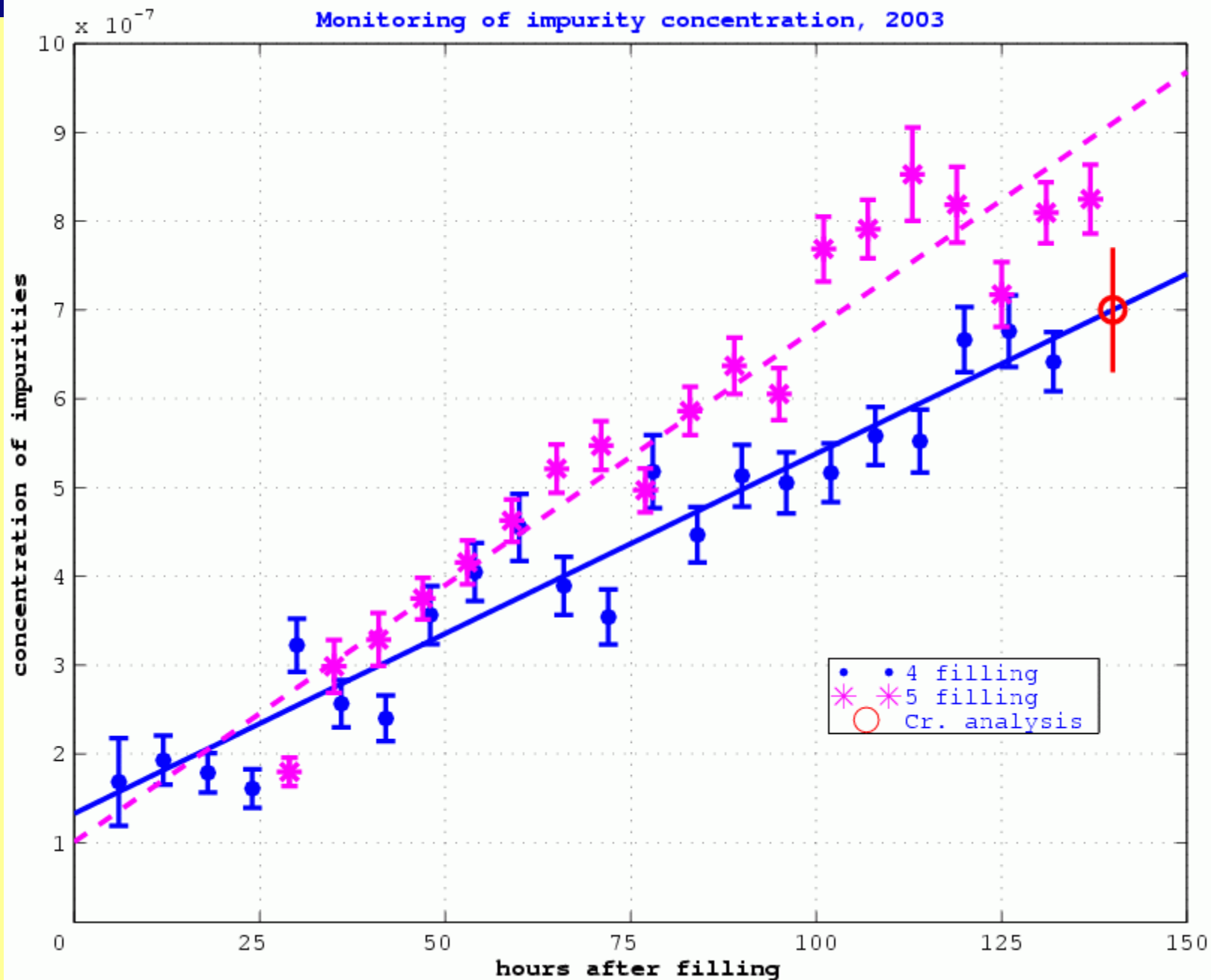


The signal on TPC anode wires from  $\mu$ -e decay event

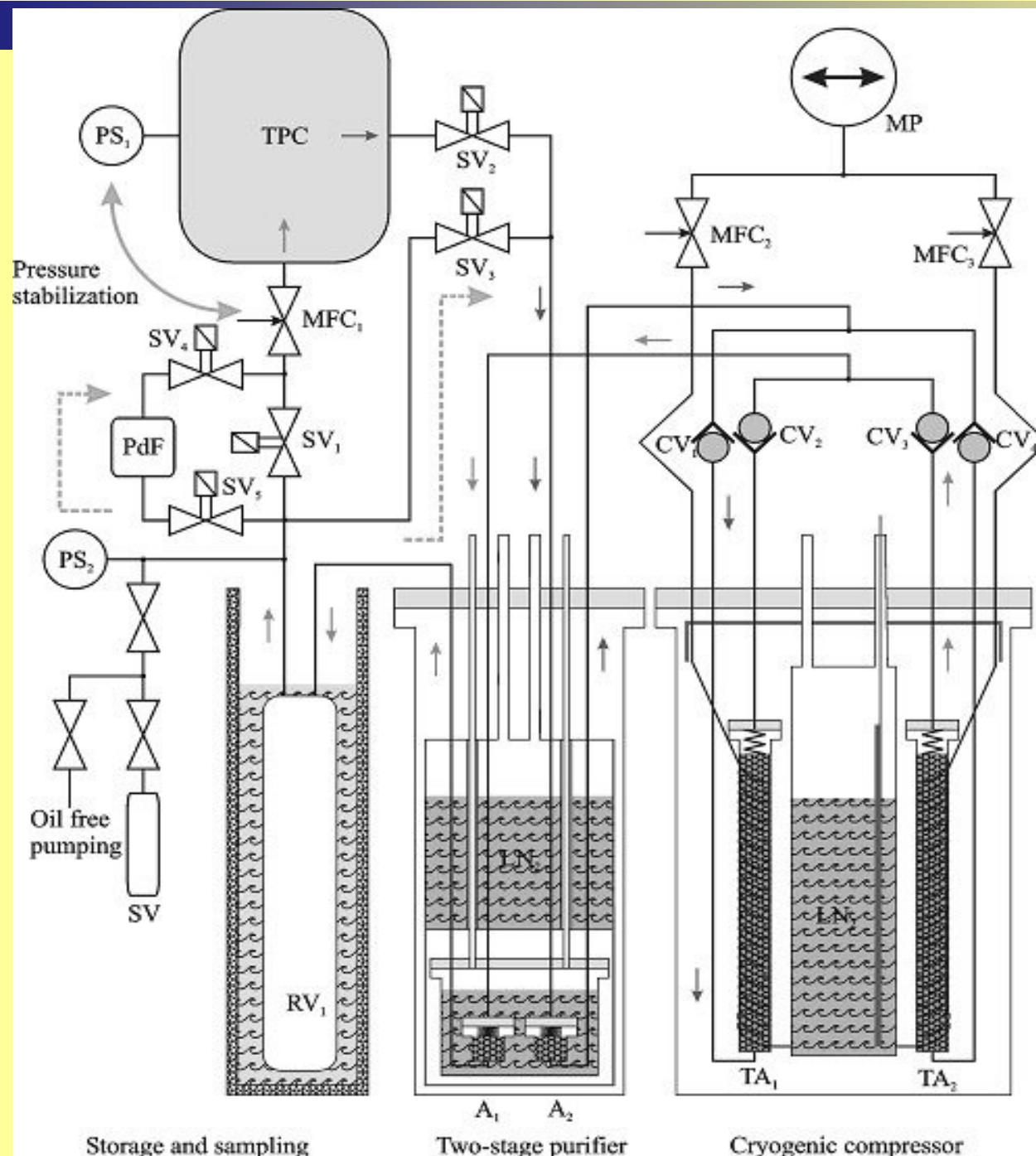


Display of a typical event with  $\mu$ -capture reaction on impurity

Monitoring of impurity concentration, 2003





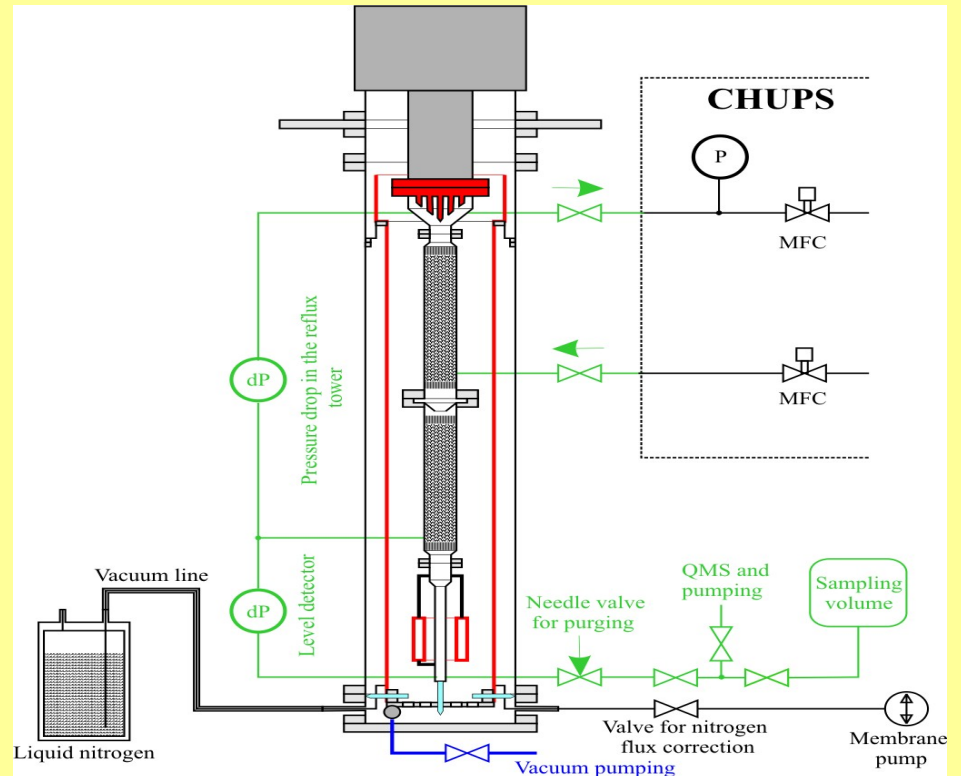


Storage and sampling

Two-stage purifier

Cryogenic compressor

# IV. the new protium isotope separation facility: production of ultra-depleted protium

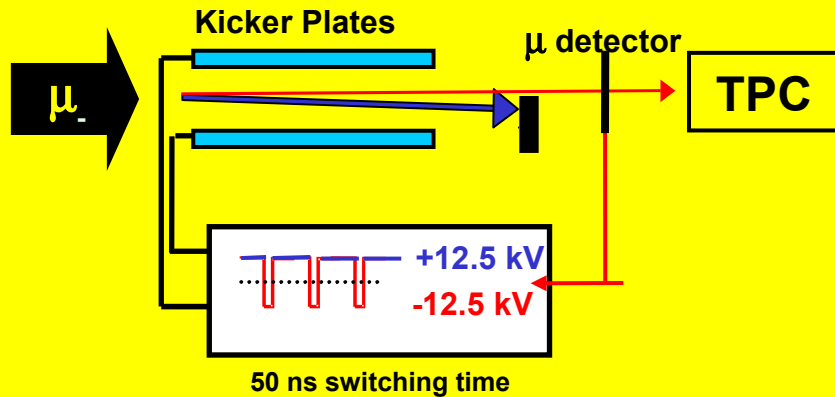


- 1) Cd = 1440 ppb (2004)
- 2) Cd < 60 ppb (2006)
- 3) Cd < 6 ppb (2007)

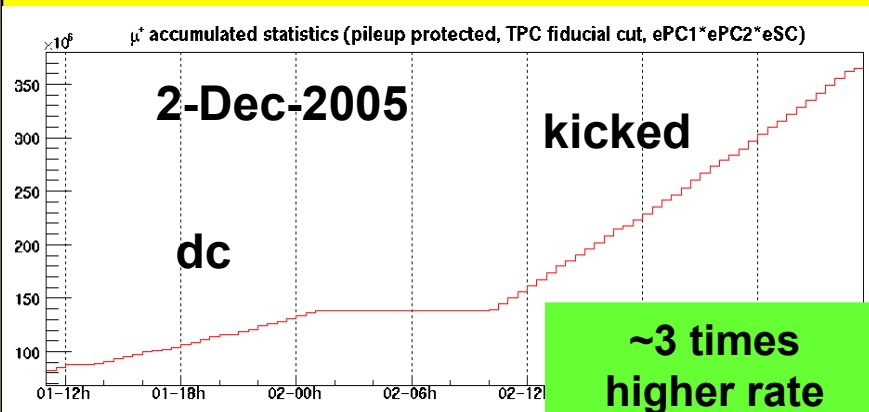


- Single muon requirement (to prevent systematics from pile-up)
- limits accepted  $\mu$  rate to  $\sim 7$  kHz,
- while PSI beam can provide  $\sim 70$  kHz

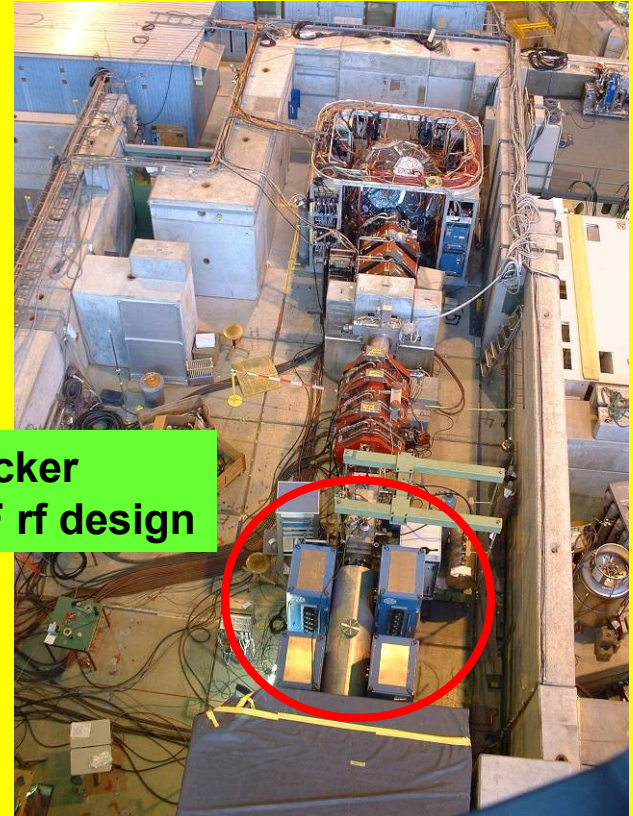
## ■ Muon-On-Demand concept

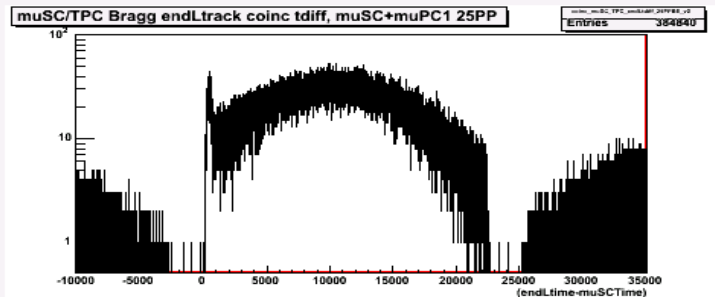
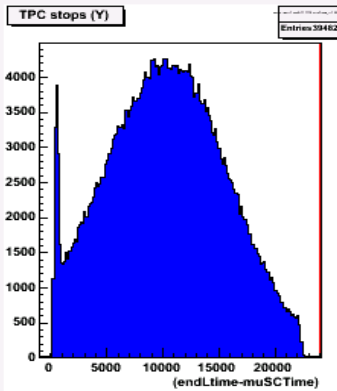
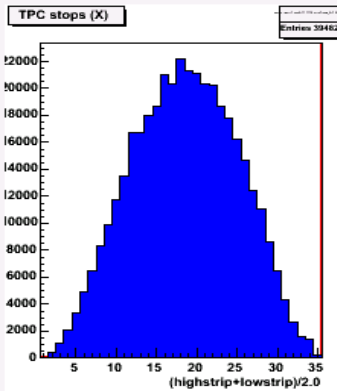
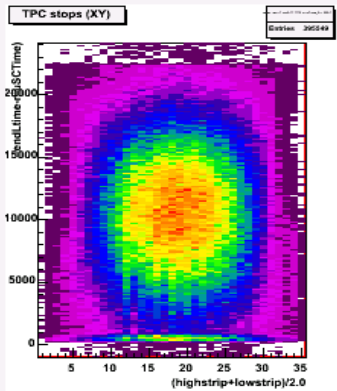
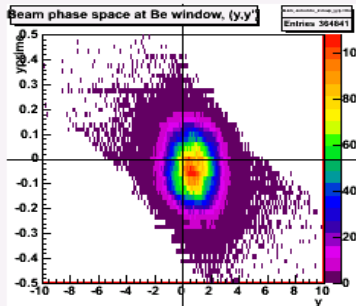
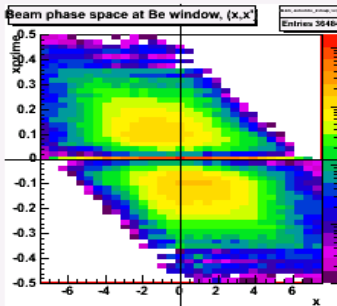
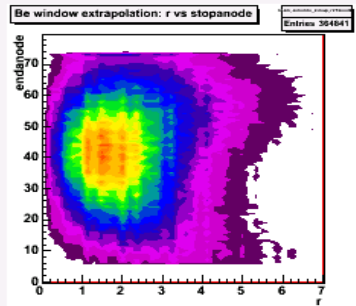
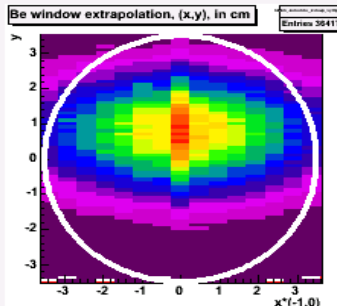
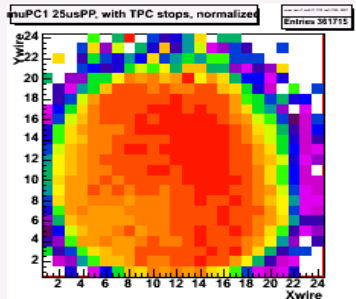
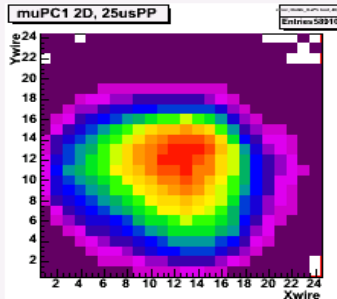
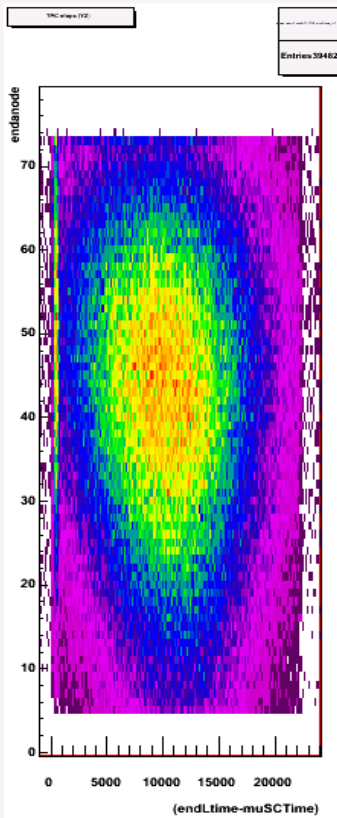
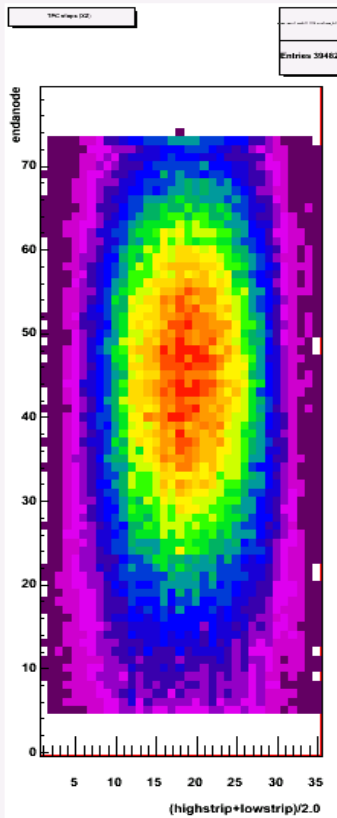
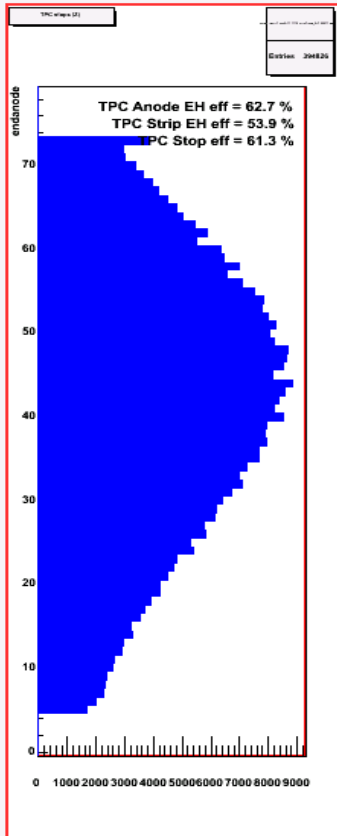


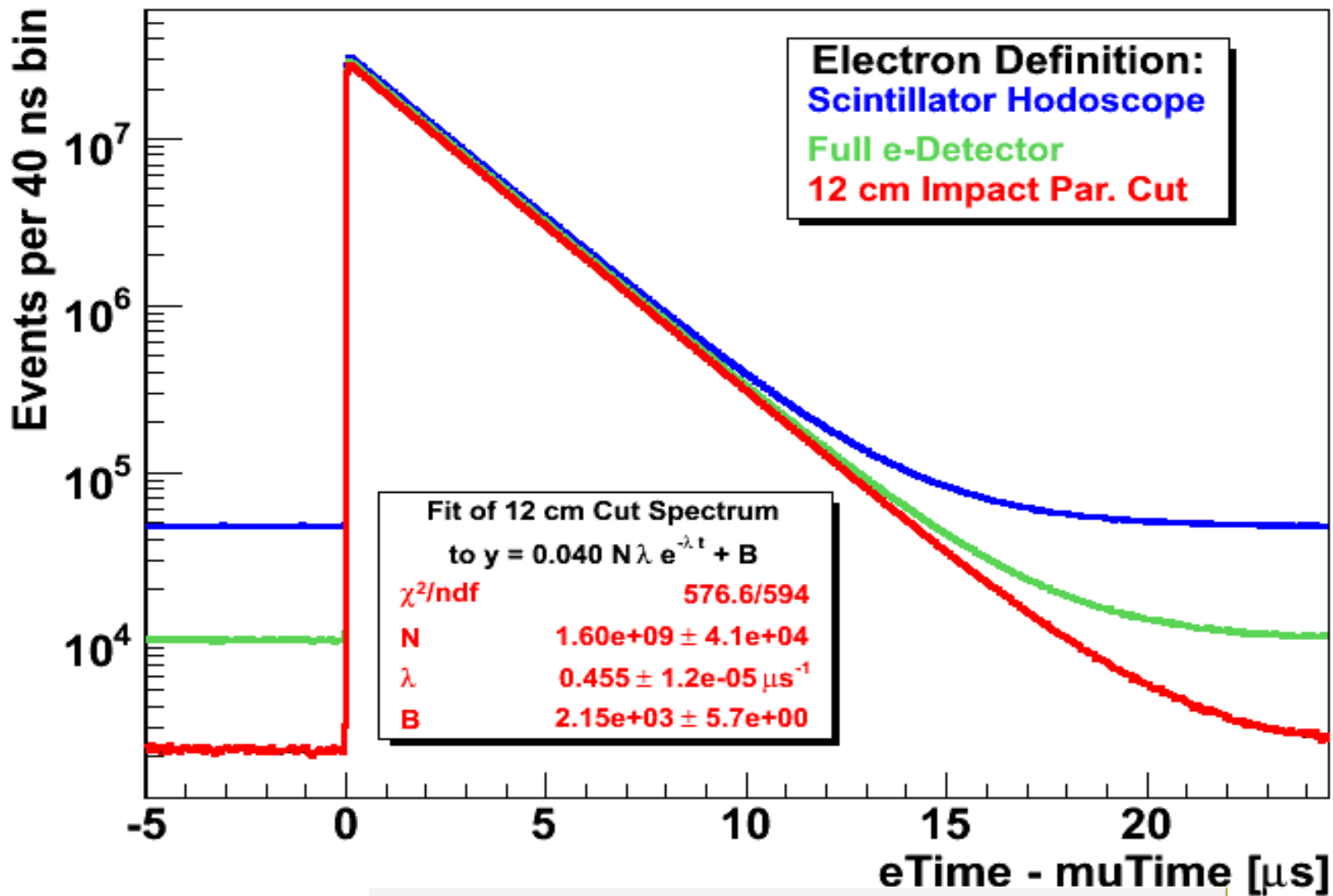
50 ns switching time



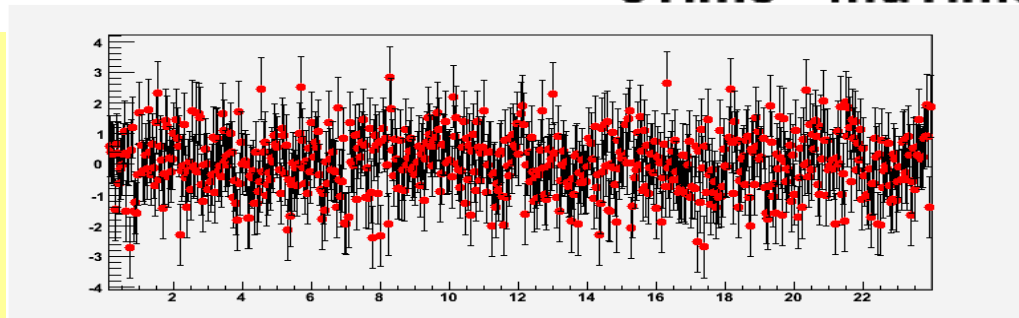
## ■ Beamline







Normalized residuals



## Общая набранная статистика

Год	$\mu^+$ ( $10^9$ )	$\mu^-$ ( $10^9$ )	Cd(ppb)	H2O(ppb)
2004	0.2	2.0	~1400	~70
2005	1.4	3.5	~1400	36
2006	1.56	8.6	<60	18
2007	5.4	6.0	<6	8.7

Общий объем данных за 2004-2007 гг. ~ 100 TB

8.56

20.1

**TABLE: Applied corrections and systematic errors.**

<b>Effect</b>	<b>Corrections and uncertainties [s-1]</b>	
	<b>R06</b>	<b>R07</b>
<b>Z &gt; 1 impurities</b>	<b>7.8 + - 1.9</b>	<b>4.5 + - 0.9</b>
<b>mu-p scatter removal</b>	<b>12.4 + - 3.2</b>	<b>7.2 + - 1.3</b>
<b>mu-p diffusion</b>	<b>3.1 + - 0.1</b>	<b>3.0 + - 0.1</b>
<b>mu-d diffusion</b>	<b>+ - 0.7</b>	<b>+ - 0.1</b>
<b>Fiducial volume cut</b>	<b>+ - 3.0</b>	<b>+ - 3.0</b>
<b>Entrance counter ineff.</b>	<b>+ - 0.5</b>	<b>+ - 0.5</b>
<b>Electron track def.</b>	<b>+ - 1.8</b>	<b>+ - 1.8</b>
<b>Total corr. <math>\lambda_{\mu^-}</math></b>	<b>23.3 + - 5.2</b>	<b>14.7 + - 3.9</b>
=====		
<b>mup bound state ( <math>D_{\mu p}</math> )</b>	<b>12.3 + - 0.0</b>	<b>12.3 + - 0.0</b>
<b>ppmu states ( <math>D_{pp\mu}</math> )</b>	<b>17.7 + - 1.9</b>	<b>17.7 + - 1.9</b>

## Результаты анализа данных за 2004-2007 год

$$N_{\mu^-} = 1.2 \times 10^{10}$$

$$\lambda_{\mu^-} = 455851.4 \pm 12.5_{\text{stat}} \pm 8.5_{\text{syst}} \text{ s}^{-1} \text{ (MuCAP 2004).}$$

$$\lambda_{\mu^-} = 455857.3 \pm 7.7_{\text{stat}} \pm 5.1_{\text{syst}} \text{ s}^{-1} \text{ (MuCAP 2006).}$$

$$\lambda_{\mu^-} = 455853.1 \pm 8.3_{\text{stat}} \pm 3.9_{\text{syst}} \text{ s}^{-1} \text{ (MuCAP 2007).}$$

# Muon Capture Rate $\lambda_s$

$$\lambda_s = \lambda_{\mu^-} - (\lambda_{\mu^+} - D_{\mu p}) + D_{pp\mu}$$

$$D_{\mu p} = 12.3 \text{ s}^{-1} \quad (\mu p \text{ bound state})$$

$$D_{pp\mu} = 17.7 \text{ s}^{-1} \quad (\lambda_{pp\mu} = (1.94 \pm 0.06) \mu\text{s}^{-1})$$

## Результаты анализа данных за 2004-2007 год

$$\lambda_{\mu^+} = 455170.05 \pm 0.46 \text{ s}^{-1} \text{ (}\mu\text{LAN experiment)}$$

$$\lambda_{\mu^-} = 455854.9 \pm 5.4\text{stat} \pm 4.7\text{syst} \text{ s}^{-1} \text{ (MuCap 2004-2007)}$$

$$\Lambda_S^{\text{MuCap(aver.)}} = 714.9 \pm 5.4\text{stat} \pm 5.3\text{syst} \text{ s}^{-1}$$

$$\Lambda_S^{\text{Th}} = 693.3 \text{ s}^{-1} \text{ (aver.)} + 19.4\text{s}^{-1} \text{ (r.c.)} = 712.7 \pm 3.0 \pm 3.0 \text{ s}^{-1}$$

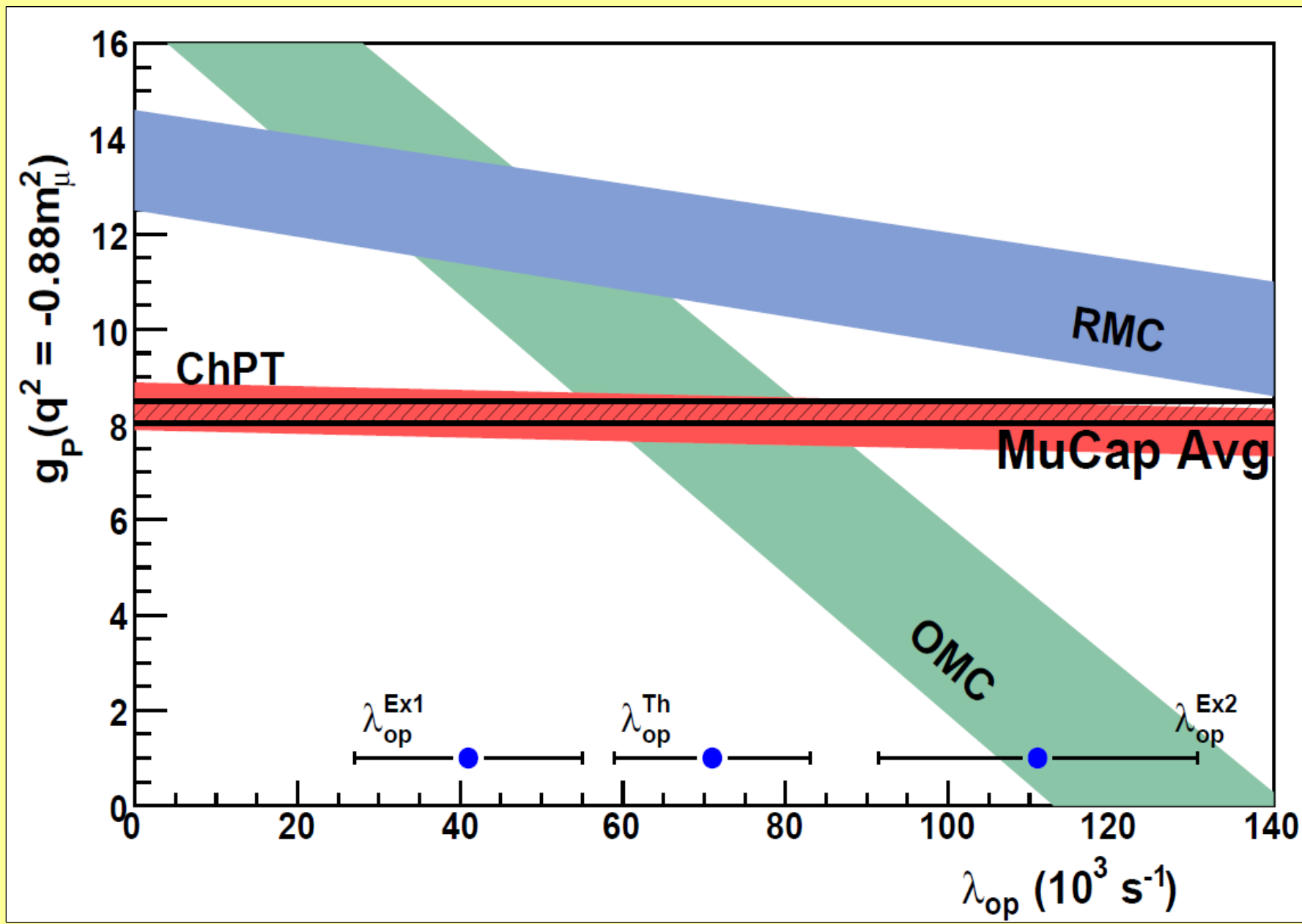
$$g_P^{\text{MuCap}} = g_P^{\text{Th}} - 0.065 \times (\Lambda_S^{\text{MuCap}} - \Lambda_S^{\text{Th}})$$

$$g_P^{\text{MuCap}} = 8.06 \pm 0.48(\text{exp}) \pm 0.28(\text{th})$$

$$g_P^{\text{Th}} = 8.2 \pm 0.2 \text{ (2.8\%)}$$



# Precise and unambiguous MuCap result solves longstanding puzzle





***MuCap collaboration***

***Petersburg Nuclear Physics Institute (PNPI), Gatchina, Russia***

***Paul Scherrer Institute (PSI), Villigen, Switzerland***

***University of California, Berkeley (UCB and LBNL), USA***

***University of Illinois at Urbana-Champaign (UIUC), USA***

***Université Catholique de Louvain, Belgium***

***TU München, Garching, Germany***

***University of Kentucky, Lexington, USA***

***Boston University, USA***

Earlier, in 1998, we have studied the muon capture on  ${}^3\text{He}$ . The muon capture rate in the channel  $\mu^- + {}^3\text{He} \rightarrow {}^3\text{H} + \nu_\mu$  was measured with high precision :

$$\Lambda_c = 1496.0 \pm 4.0 \text{ s}^{-1} \text{ (0.3\%)} .$$

This result have been used in some theoretical analyses :

L.E. Marcucci et al. (2012) [1] and D. Gazit( 2009) [2]

for deriving the  $\Lambda_c$  and the proton's pseudoscalar form factor  $g_p$ .

$$\Lambda_c = 1494 \pm 21 \text{ s}^{-1} \text{ [1] and } \Lambda_c = 1499 \pm 12 \text{ s}^{-1} \text{ ([2].}$$

$$g_p = 8.13 \pm 0.6 \text{ [2]}$$