

DOES PENTAQUARK θ^+ EXIST?

(Viewing from HEPD)

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Model by Diakonov, Petrov, and Polyakov

- Anti-decuplet of pentaquarks

$$M = (1.89 - 0.18 \cdot Y) \text{ GeV}/c^2, \quad Y = B + S, \quad Q = T_3 + Y/2.$$

Mass of N dublet is put equal to $1710 \text{ GeV}/c^2$.

Quark content: $\theta^+ = uud\bar{d}\bar{s}$. Quantum numbers: $B = 1$,
 $S = 1$, $Y = 2$, $T = 0$, $J^P = \frac{1}{2}^+$

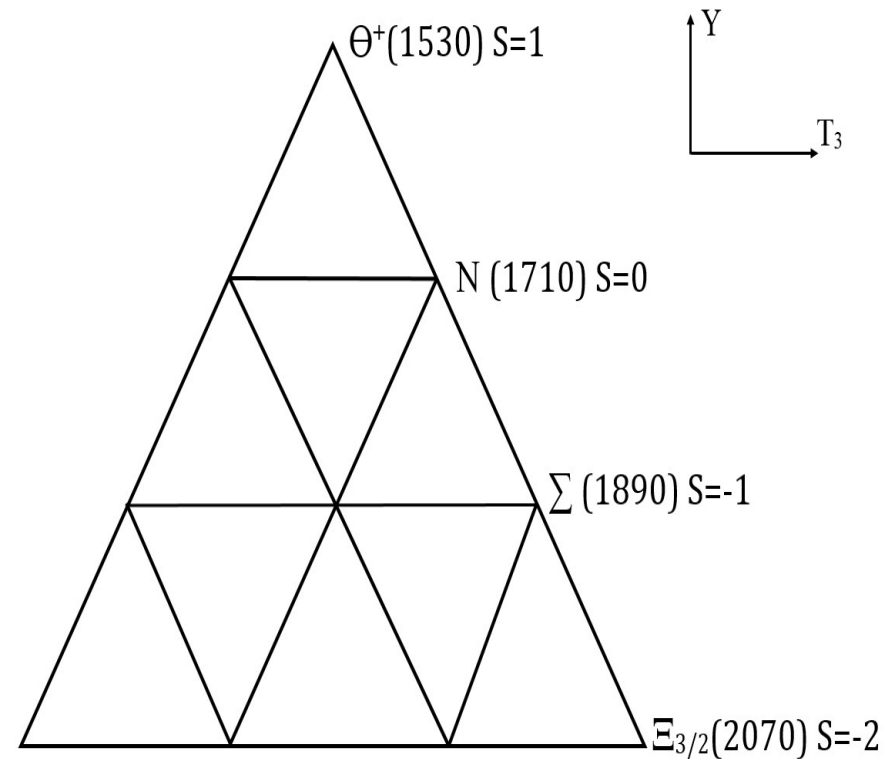
Model parameters are fixed by parameters of meson octet, baryon octet and decuplet, and the mass of $N(1710)$.

Then $M_{\theta^+} = 1.53 \text{ GeV}/c^2$,

$\Gamma_{tot} < 15 \text{ MeV}/c^2$.

θ^+ is stable particle when fig-pen-01.eps

$M_{\theta^+} < M_N + M_K$, since $\theta^+ \rightarrow n + K^+$ and $\theta^+ \rightarrow p + K^0$.



First Evidences that θ^+ Exists

- First data in 2003 year

- LEPS Collaboration, Phys. Rev. Lett. 91 (2003) 012002.

Reaction $\gamma + n \rightarrow \theta^+ + K^- \rightarrow K^+ + K^- + X$ on ^{12}C ,

Assumed $X = n$, $0.9 < M_X < 0.98 \text{ GeV}/c^2$.

$M_{\theta^+} = (1.54 \pm 0.01) \text{ GeV}/c^2$, $\Gamma_{tot} < 25 \text{ MeV}/c^2$,

significance $S/\sqrt{B} = 19.0/\sqrt{17.0} = 4.6\sigma$,

but $S/\sqrt{S+B} = 3.2\sigma$.

- DIANA Collaboration, Phys. At. Nucl. 66 (2003) 1715.

Reaction $K^+ + Xe \rightarrow p + \pi^+ + \pi^- + X$,

Subprocess $K^+ + n \rightarrow \theta^+ \rightarrow p + K^0$, $K_S^0 \rightarrow \pi^+ + \pi^-$.

$M_{\theta^+} = (1.539 \pm 0.002) \text{ GeV}/c^2$, $\Gamma_{tot} < 9 \text{ MeV}/c^2$,

significance $S/\sqrt{B} = 29/\sqrt{44} = 4.4\sigma$.

First Evidences that θ^+ Exists

- CLAS Collaboration, Phys. Rev. Lett. 91 (2003) 252001.

Reaction $\gamma + d \rightarrow K^+ + K^- + p + n$.

$M_{\theta^+} = (1.542 \pm 0.005) \text{ GeV}/c^2$, $\Gamma_{tot} < 21 \text{ MeV}/c^2$,

significance $S/\sqrt{B} = 43/\sqrt{54} = (5.2 \pm 0.6)\sigma$.

- SAPHIR Collaboration, Phys. Lett. B572 (2003) 127.

Reaction $\gamma + p \rightarrow \bar{K}^0 + \theta^+ \rightarrow \bar{K}^0 + K^+ + n$,

oscillation $\bar{K}^0 \rightarrow K_S^0 + K_L^0$, decay $K_S^0 \rightarrow \pi^+ + \pi^-$.

$M_{\theta^+} = (1.540 \pm 0.004 \pm 0.002) \text{ GeV}/c^2$, $\Gamma_{tot} < 25 \text{ MeV}/c^2$,

significance 4.8σ , $N_{\theta^+} = 63 \pm 13$, $\sigma_{\theta^+} = 300 \text{ nb}$.

First Evidences that θ^+ Exists

- Bandwagon effects (after 2003 year)
- Neutrino experiments WA21, WA25, WA59, E180, E632, (CERN and Fermilab data were reanalyzed)

Phys. At. Nucl. 67 (2004) 682.

Reaction $\nu_\mu(\bar{\nu})_\mu + T \rightarrow K_S^0 + p + X, K_S^0 \rightarrow \pi^+ + \pi^-$,
 $T = p, d, Ne - H_2$ mix.

$M_{\theta^+} = (1.533 \pm 0.005) \text{ GeV}/c^2, \Gamma_{tot} < 20 \text{ MeV}/c^2,$

significance 6.7σ .

- HERMES Collaboration, Phys. Lett. B585 (2004) 213.

Reaction $\gamma + d \rightarrow K_S^0 + p + X, X = n, K_S^0 \rightarrow \pi^+ + \pi^-$.

$M_{\theta^+} = (1.528 \pm 0.0026 \pm 0.0021) \text{ GeV}/c^2,$

$\Gamma_{tot} < 4.3 \text{ MeV}/c^2,$

significance $(3.4 \div 6.3)\sigma$.

Vanishing Pentaquarks

- Null and Negative Results

- CLAS negative result (no θ^+ signal)

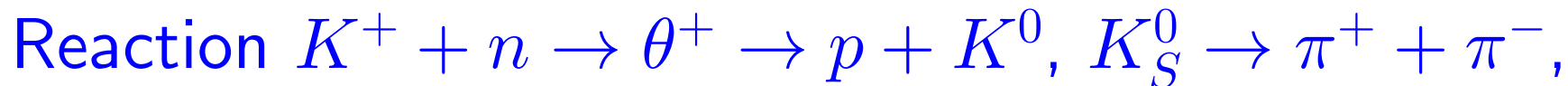
CLAS against SAPHIR data for the same reaction



$$\sigma_{\theta^+} = \sigma(\gamma + p \rightarrow \theta^+ + \bar{K}^0) < 0.8 \text{ nb}, L = 70 \text{ pb}^{-1},$$

$$N_{\theta^+} = L\sigma_{\theta^+} = 56000. \text{ SAPHIR: } \sigma_{\theta^+} = 300 \text{ nb}.$$

- Belle null result



$$\sigma(\theta^+)/\sigma(\Lambda(1520)) < 0.02, N_{obs}(\Lambda(1520)) = 15519 \pm 412.$$

For $M_{\theta^+} = 1540 \text{ MeV}, N(\theta^+) = 29 \pm 65,$

$$N(\theta^+) < 94 \text{ at } 90\% \text{ CL}.$$

Vanishing Pentaquarks

- Bandwagon effects of not to observe the θ^+ pentaquark
- HERMES Collaboration, Phys. Lett. B585 (2004) 213.
Phys. Rev. D91 (2015) 057101

The same reaction $\gamma + d \rightarrow K_S^0 + p + X, K_S^0 \rightarrow \pi^+ + \pi^-$.

Previous: $M_{\theta^+} = 1.528 \text{ GeV}/c^2, \Gamma_{tot} < 4.3 \text{ MeV}/c^2,$

significance $(3.4 \div 6.3)\sigma$.

New: $M_{\theta^+} = 1.522 \text{ GeV}/c^2, N_{\theta^+} = 68_{-31}^{+98}(stat) \pm 13(sys).$

significance 2σ .

- But LEPS and DIANA insist on the θ^+ observation
LEPS 2019: $\gamma + d \rightarrow K^+ + K^- + p + n$ significance 3σ .
DIANA 2018 study angular distribution: significance 7.1σ .
- None discovery can be made by majority voting

Coherent Background

- Ignorance of coherence in data processing

Example: reaction $\gamma + d \rightarrow K^+ + K^- + p + n$.

Signal: $\gamma + n \rightarrow \theta^+ + K^- \rightarrow (K^+ + n) + K^-$.

Amplitude F_{θ^+} . Proton spectator.

First background process:

$\gamma + d \rightarrow \phi + p + n \rightarrow (K^+ + K^-) + p + n$. Amplitude F_{ϕ} .

Second background process: $\gamma + p \rightarrow \Lambda(1520) + K^+ \rightarrow (p + K^-) + K^+$. Amplitude F_{Λ^*} . Neutron spectator.

The sum of amplitudes describes the reaction cross section $\sigma \propto |F_{\theta^+} + F_{\phi} + F_{\Lambda^*} + F_{NR}|^2$, (NR - Non-Resonance) instead of the sum of subprocess cross sections

$$\sigma_{\theta^+} + \sigma_{\phi} + \sigma_{\Lambda^*} + \sigma_{NR} \propto |F_{\theta^+}|^2 + |F_{\phi}|^2 + |F_{\Lambda^*}|^2 + |F_{NR}|^2.$$

Usually the cross sections of background processes σ_{ϕ} and σ_{Λ^*} are subtracted from the cross section of the process under study (σ). This may provide false peaks.

Search for θ^+ in Hadronic Channels

- What does the CLAS negative result mean?

The cross section of θ^+ production by virtual photon is lower than the CLAS threshold of observation.

- This does not mean that θ^+ with small width does not exist, but it was not observed only in photoproduction.
- The most perspective process for searching θ^+ is hadron scattering of elementary particles.

since the largest branchings of θ^+ decay are hadronic:

$$Br(\theta^+ \rightarrow p + K^0) \text{ and } Br(\theta^+ \rightarrow n + K^+).$$

- Nuclear targets should be excluded to avoid Fermi motion and rescattering (smearing) effects.

Search for θ^+ in Hadronic Channels

- Examples of perspective hadronic reactions

$$\pi^- + p \rightarrow \theta^+ + K^-, E_\pi \geq 1.67 \text{ GeV, for } M_{\theta^+} = 1.53 \text{ GeV.}$$

$$\bar{p} + p \rightarrow \theta^+ + \bar{\theta}^-, E_{\bar{p}} \geq 4.05 \text{ GeV (PANDA).}$$

- Cross section of $\theta^+ + \bar{\theta}^-$ production in $\bar{p} + p$ collision

In the simplest model of K^0 exchange

the cross section maximum is given by

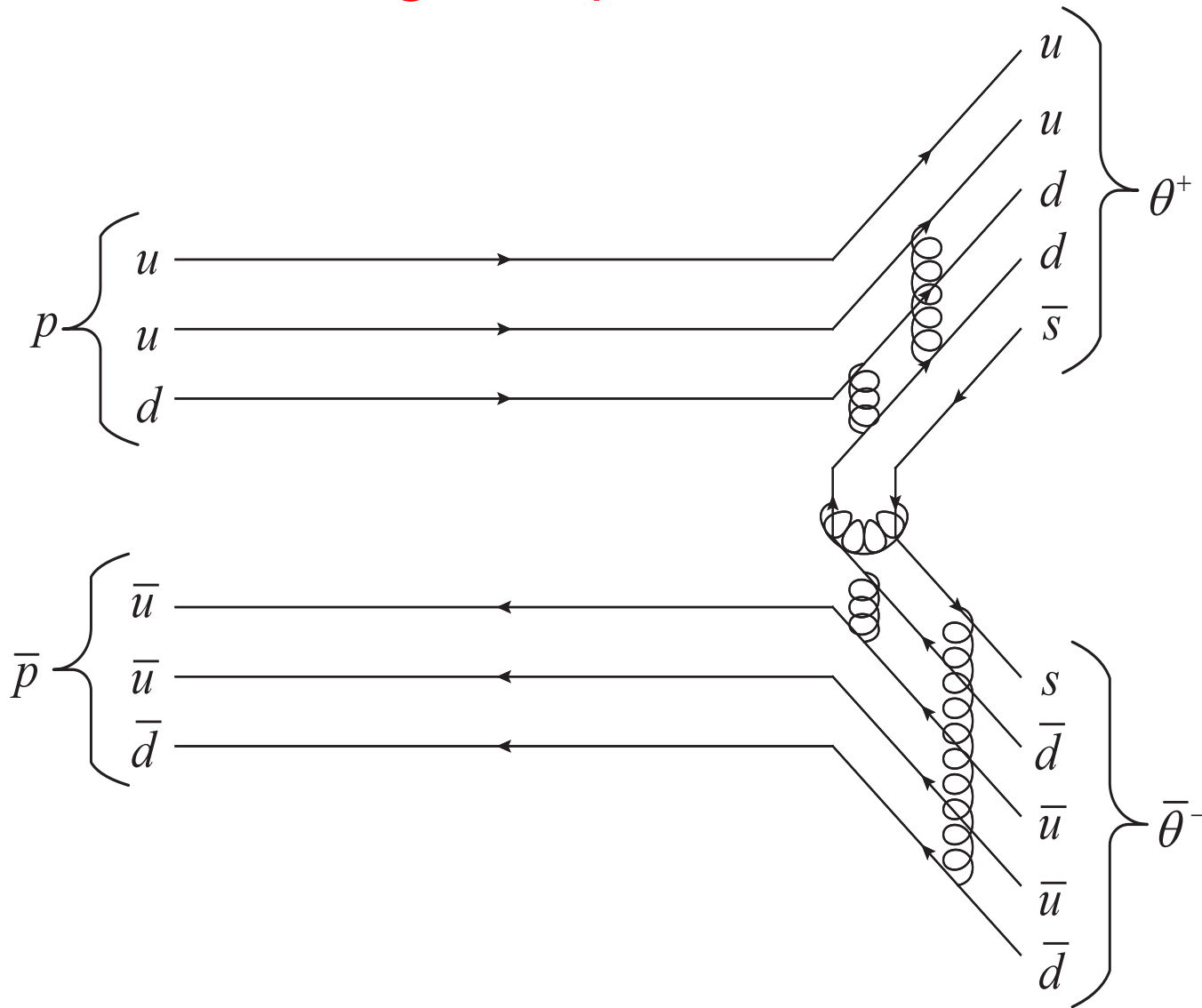
$$\sigma_s(\bar{p} + p \rightarrow \theta^+ + \bar{\theta}^-) = 0.5 \cdot (\Gamma_{tot})^2 \mu b,$$

where the total width of θ^+ is measured in MeV and the beam energy is 5 GeV.

$$\mathcal{L}_{PANDA} = 2 \cdot 10^{32} \text{ cm}^2 \text{ s}^{-1}, \dot{N} = L \cdot \sigma = 100 \cdot (\Gamma_{tot})^2 \text{ s}^{-1}.$$

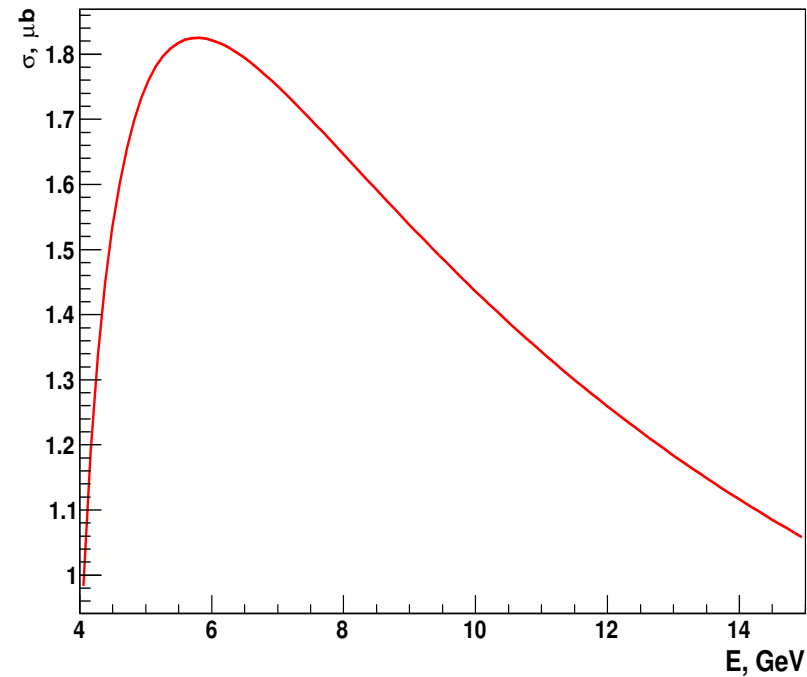
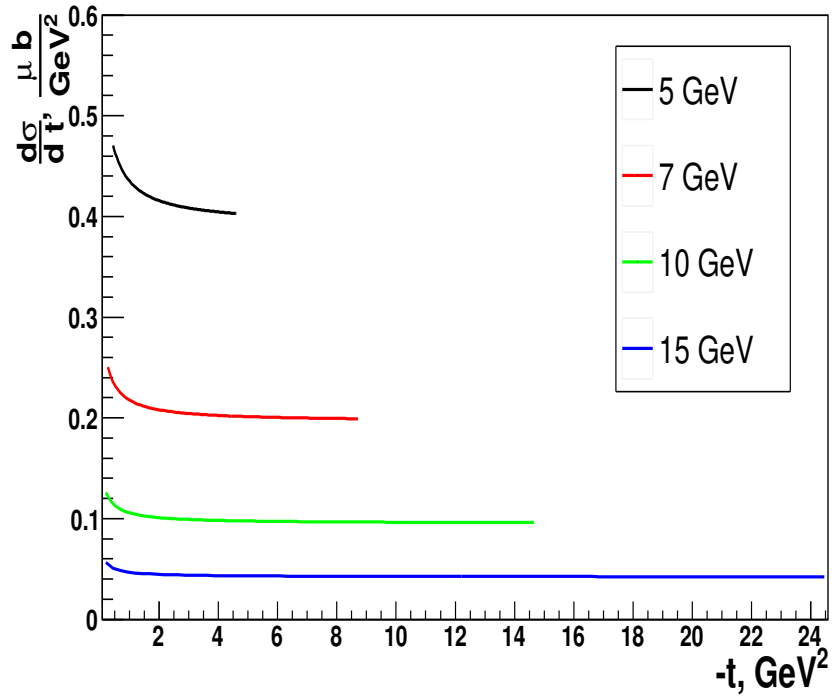
Pentaquark Production through Kaon Exchange

- Kaon Exchange Graph



Pentaquark Production through Kaon Exchange

- Differential and total cross sections



$$M_{\theta^+} = 1.53 \text{ GeV}/c^2, \Gamma_{\theta^+} = 2 \text{ MeV}/c^2$$

Requirements to Suppress Background

- Ratio R_{bg}^s of signal to background

If we put for rough estimate $\Gamma_{tot} = 1$ MeV and the total cross section of $\bar{p}p$ scattering $\sigma_{\bar{p}p}^{tot} = 50$ mb we get $R_{bg}^s = \sigma_s / \sigma_{\bar{p}p}^{tot} = 10^{-5}$.

- The main problem for PANDA experiment is to suppress the background by a factor of about $10^5 \div 10^6$.

- Reaction $\bar{p} + p \rightarrow (\bar{p} + \pi^+ + \pi^-) + (p + \pi^+ + \pi^-)$

$\text{Br}(\theta^+ \rightarrow p + K^0) \approx 0.5$, probability of transition $K^0 \rightarrow K_S^0$ is 0.5, and $\text{Br}(K_S^0 \rightarrow \pi^+ + \pi^-) \approx 0.69$.

This gives addition small factor $\approx 1/32$ for R_{bg}^s .

- Demand that the final state should contain only

$\bar{p} + p + 2\pi^+ + 2\pi^-$ reduces the cross section of background processes significantly ($\sigma_{bg} \ll \sigma_{\bar{p}p}^{tot}$)

Requirements to Suppress Background

- Choice of $\pi^+\pi^-$ pairs and cuts for K_S^0 mass

The $\pi^+\pi^-$ pairs are to be chosen in such a way that the sum of two squares $(M_{\pi^+\pi^-} - M_{K_S^0})^2$ is minimal, where $M_{K_S^0}$ is the PDG value. Restriction on maximal values of $(M_{\pi^+\pi^-} - M_{K_S^0})^2$ reduces background.

- Cuts for decay length

There are two long living particles K_S^0 in reaction:

$$\bar{p} + p \rightarrow \theta^+ + \bar{\theta}^- \rightarrow (\bar{p} + \bar{K}^0) + (p + K^0), \quad K^0 \rightarrow K_S^0.$$

Applying cuts for the minimal distances between the K_S^0 decay vertex position and the $\bar{p}p$ interaction point we can suppress background significantly.

- Collinearity cuts

Trajectories of K^0 and \bar{K}^0 are to correspond to their three-momenta. These cuts suppress background also.

Advantages of Searching θ^+ at PANDA

- Search in θ^+ Mass Region from 1217 MeV to 1834 MeV
 $2.22 \geq E_{\bar{p}} \geq 6.23$ GeV (PANDA: $1.5 \geq E_{\bar{p}} \geq 15.0$ GeV)

Molecular model: $|P_c^+ \rangle = |\Sigma_c + \bar{D}^* \rangle,$

$$|\theta^+ \rangle = \alpha |p + K^0 \rangle + \beta |n + K^+ \rangle,$$

$$|\theta^+ \rangle = \alpha |p + K^{*0} \rangle + \beta |n + K^{*+} \rangle,$$

$$\theta^+ \rightarrow p + \pi^+ + \pi^-, \quad M_{\theta^+} \geq m_p + 2m_{\pi^+} = 1217 \text{ MeV}$$

$$\theta^+ \rightarrow n + K^+, \quad M_{\theta^+} \geq m_n + M_{K^+} = 1433 \text{ MeV.}$$

$$\theta^+ \rightarrow p + K^{*0}, \quad M_{\theta^+} \geq m_p + M_{K^{*0}} = 1834 \text{ MeV.}$$

- High statistics experiment:

$$\dot{N}_D = \epsilon_D L \cdot \sigma_s = \epsilon_D \cdot 100 \cdot (\Gamma_{tot})^2 \text{ s}^{-1}, \quad \epsilon_D \sim 1\%.$$

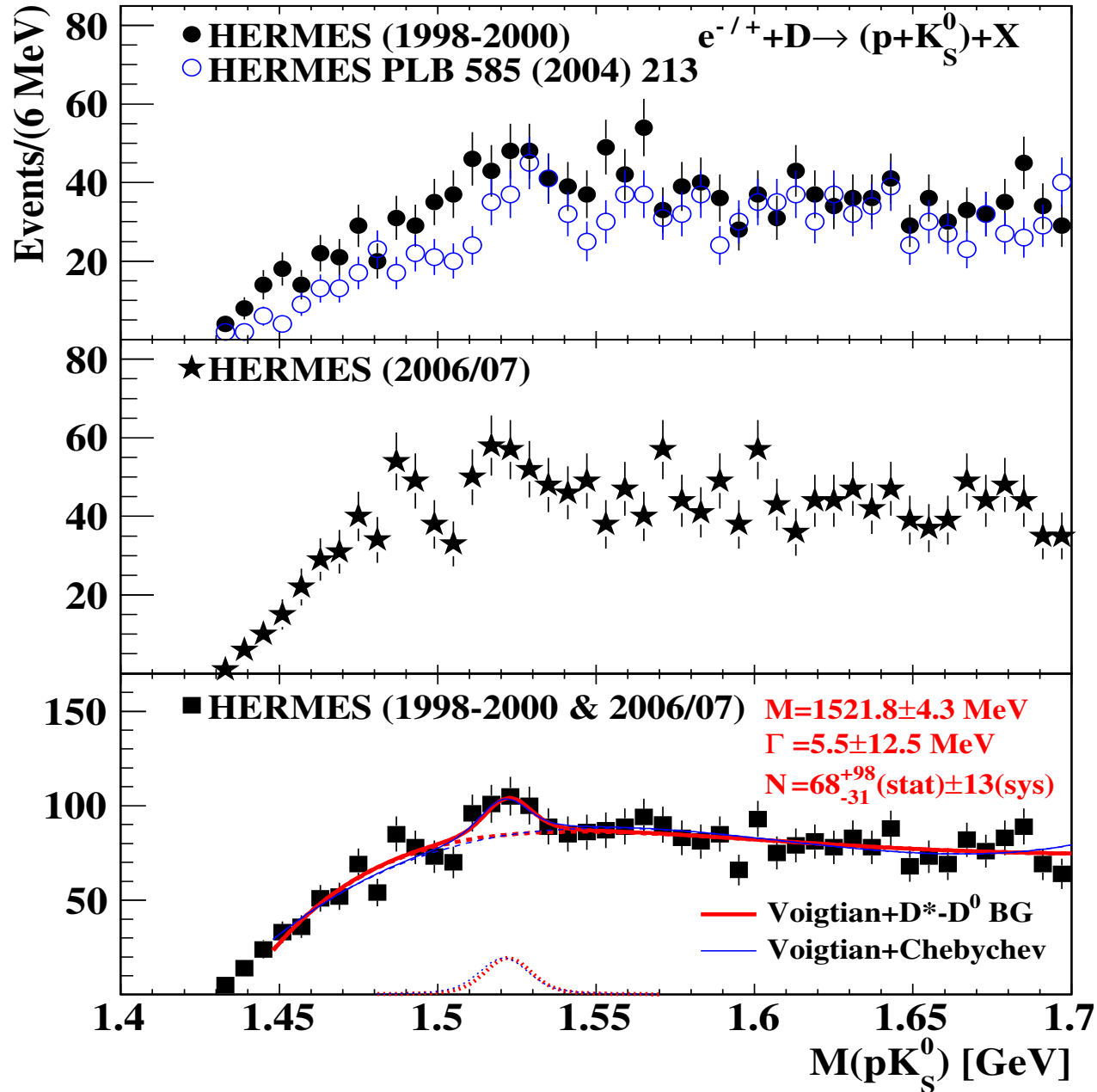
- Possibility to establish strangeness

$$\bar{p} + p \rightarrow \theta^+ + \bar{\theta}^-, \quad \theta^+ \rightarrow n + K^+, \quad \bar{\theta}^- \rightarrow \bar{p} + \bar{K}^0.$$

Conclusions

- Neither existence nor non-existence of the θ^+ pentaquark is not established now
- Search in wide region of θ^+ mass should be performed
- It is desirable not to use nuclear targets to avoid the Fermi motion and rescattering effect contributions
- It is highly likely that the most perspective reactions for θ^+ production are hadronic ones
- Production rate for the θ^+ pentaquark in the PANDA experiment can be about a few events per second
- Search for the θ^+ pentaquark at PANDA can be realized in wide mass region even below kaon production threshold
- The most serious problem of the PANDA experiment is to find effective requirements to suppress background process contributions

Backup Slides



Backup Slides

- Differential Cross Section for $\theta^+\bar{\theta}^-$ Production

$$\frac{d\sigma}{dt} = \frac{g^4[(M_\theta - m_N)^2 - t]^2}{16\pi s(s - 4m_N^2)(M_K^2 - t)^2}$$

- Total Cross Section for $\theta^+\bar{\theta}^-$ Production $\sigma_{tot} =$

$$\frac{g^4}{16\pi s(s - 4m_N^2)} \left\{ [(M_\theta - m_N)^2 - M_K^2]^2 \left[\frac{1}{M_K^2 - t_{min}} - \frac{1}{M_K^2 - t_{max}} \right] + 2[(M_\theta - m_N)^2 - M_K^2] \ln \left[\frac{M_K^2 - t_{max}}{M_K^2 - t_{min}} \right] + t_{min} - t_{max} \right\}.$$

Here $(-t_{max})/(-t_{min})$ is maximal/minimal value of $(-t)$.

- Total Width of the Pentaquark Decay $\theta^+ \rightarrow N + K$

$$\Gamma_{tot} = \frac{g^2[(M_\theta - m_N)^2 - M_K^2]}{4\pi M_\theta^2} P_0 \equiv \frac{g^2 P_0^3}{\pi[(M_\theta + m_N)^2 - M_K^2]},$$

where $P_0 = \frac{\sqrt{[(M_\theta - m_N)^2 - M_K^2][(M_\theta + m_N)^2 - M_K^2]}}{2M_\theta}$.